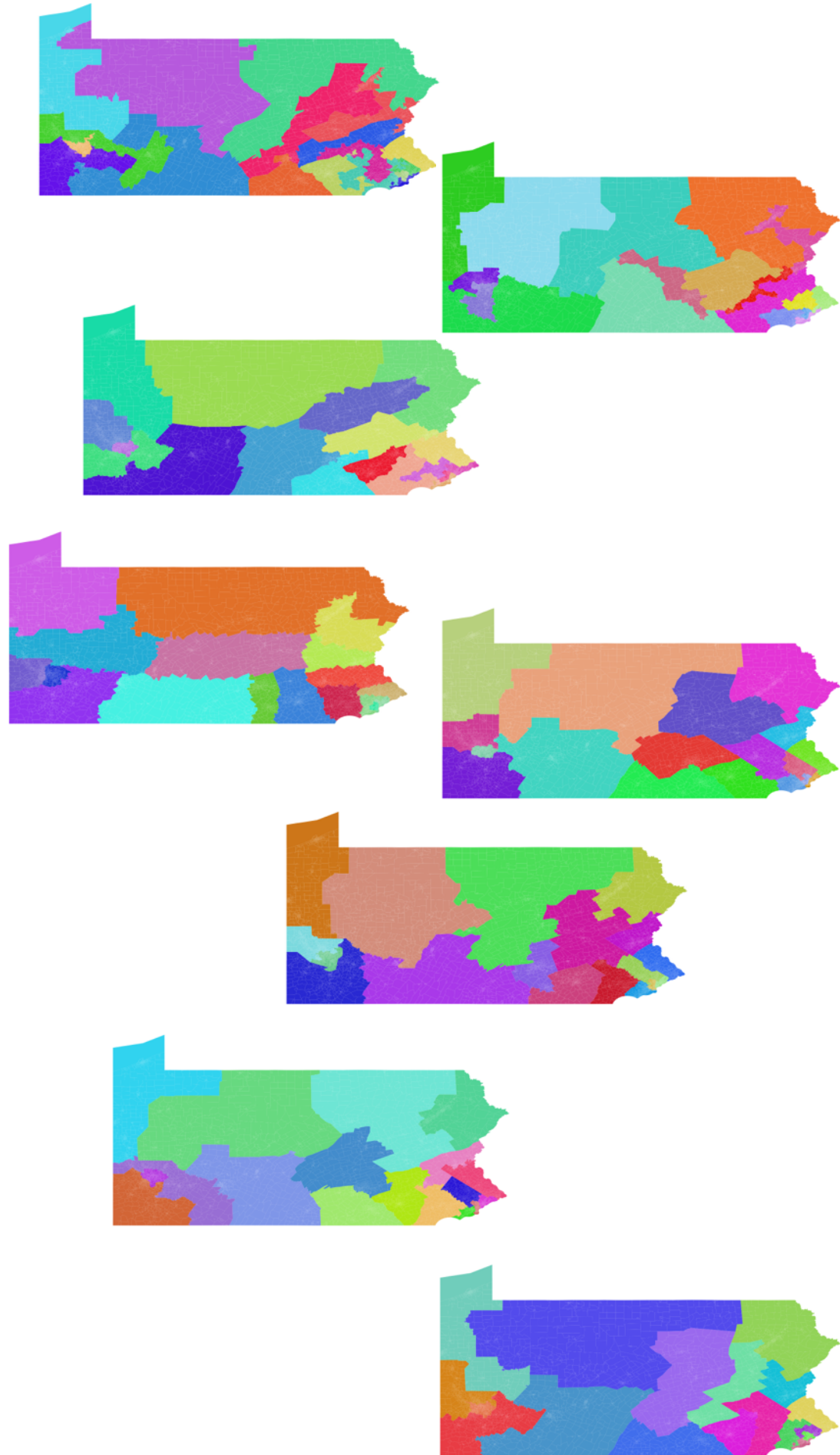


MOON DUCHIN

WHAT EVEN IS
PENNSYLVANIA?



MOON DUCHIN

**WHAT EVEN IS
(FAIR IN)
PENNSYLVANIA?**

ENTITIES

NATION, STATE, DISTRICT

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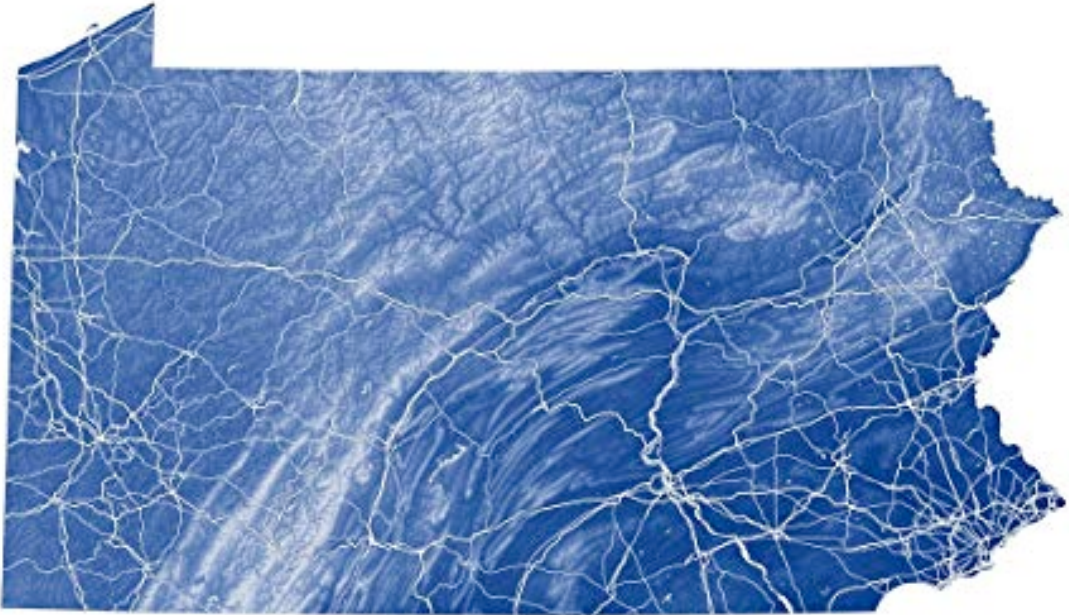
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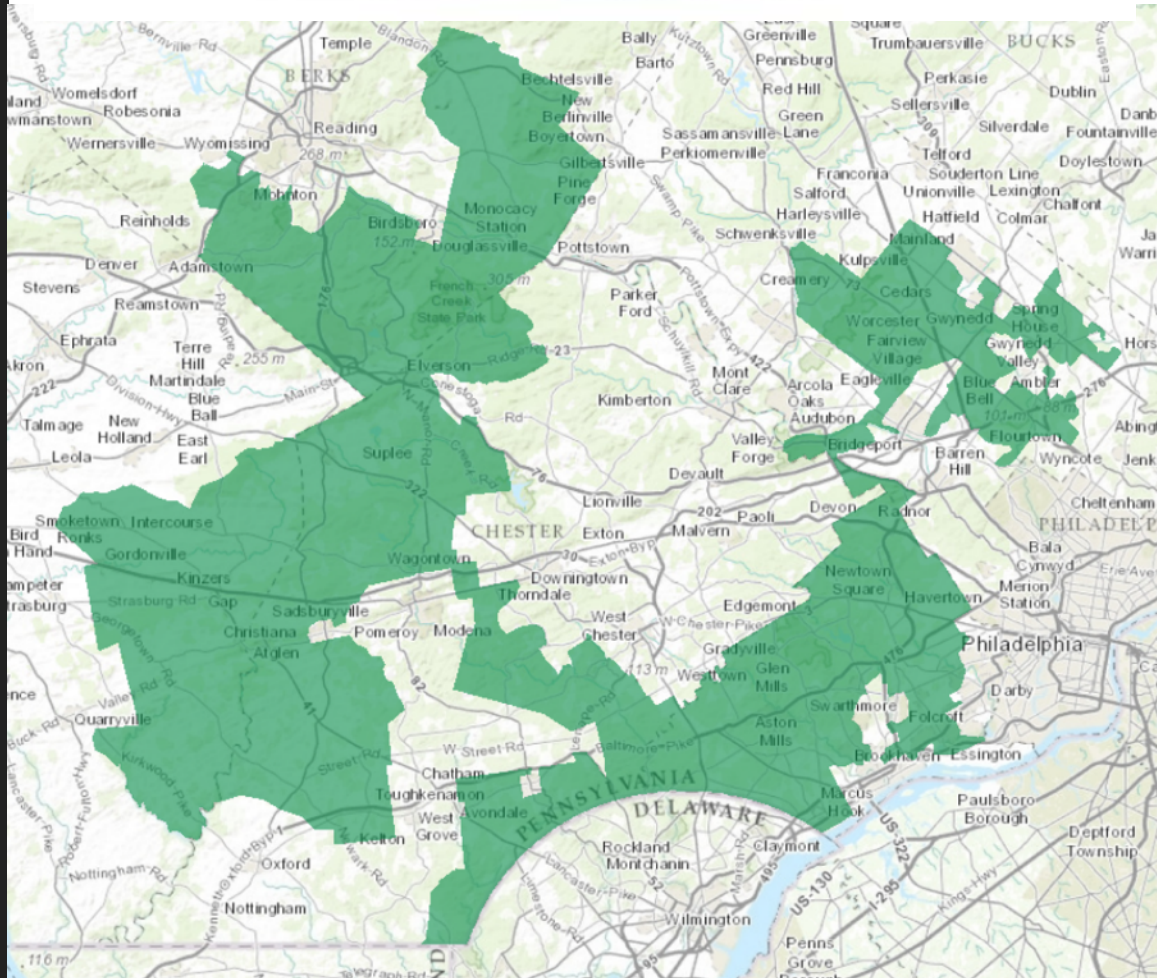
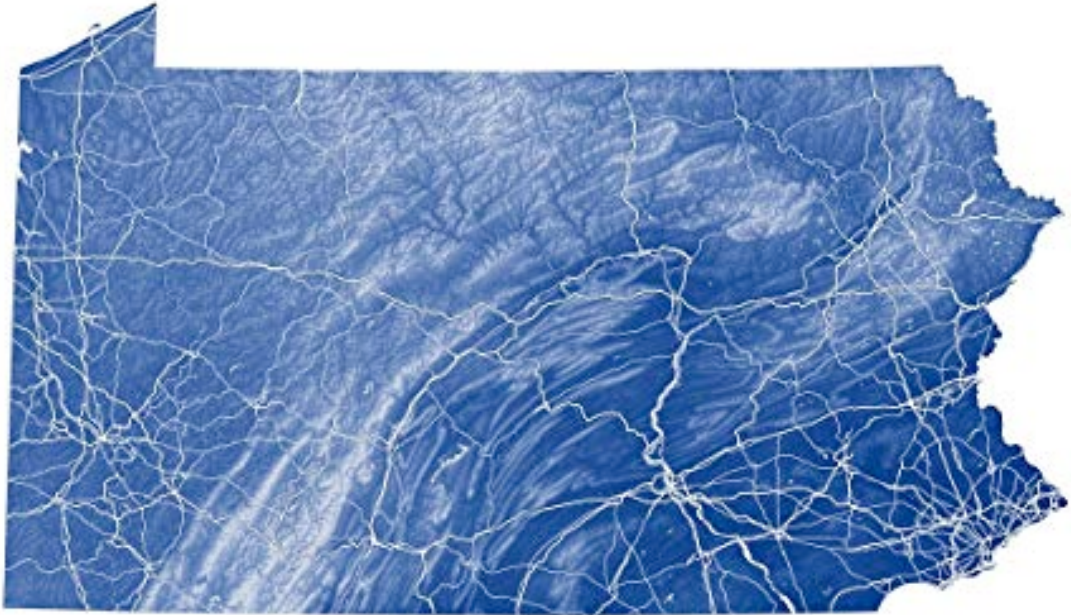
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- ▶ The United States is the only country in the world that
(a) mandates regular re-drawing of districts, and
(b) puts (partisan) elected officials in charge.



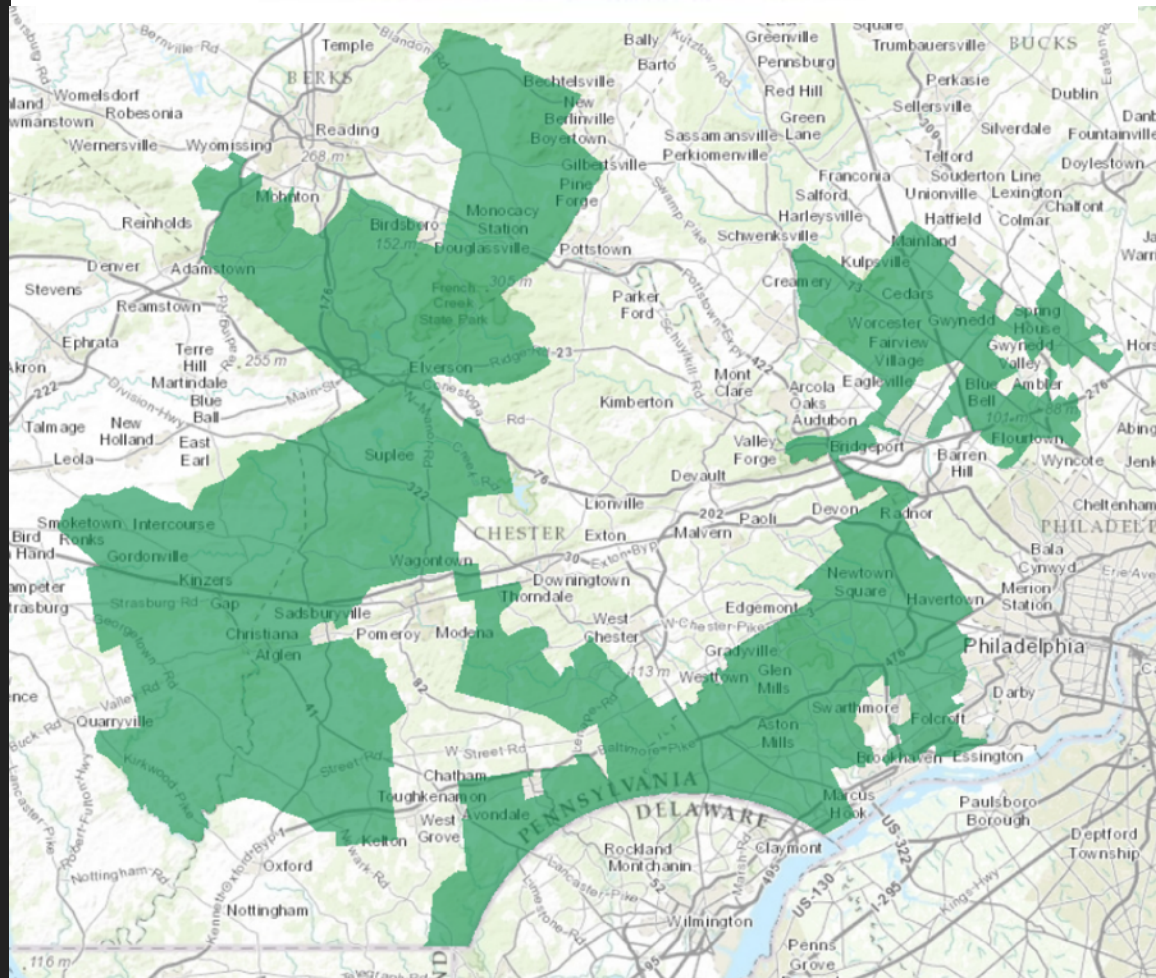
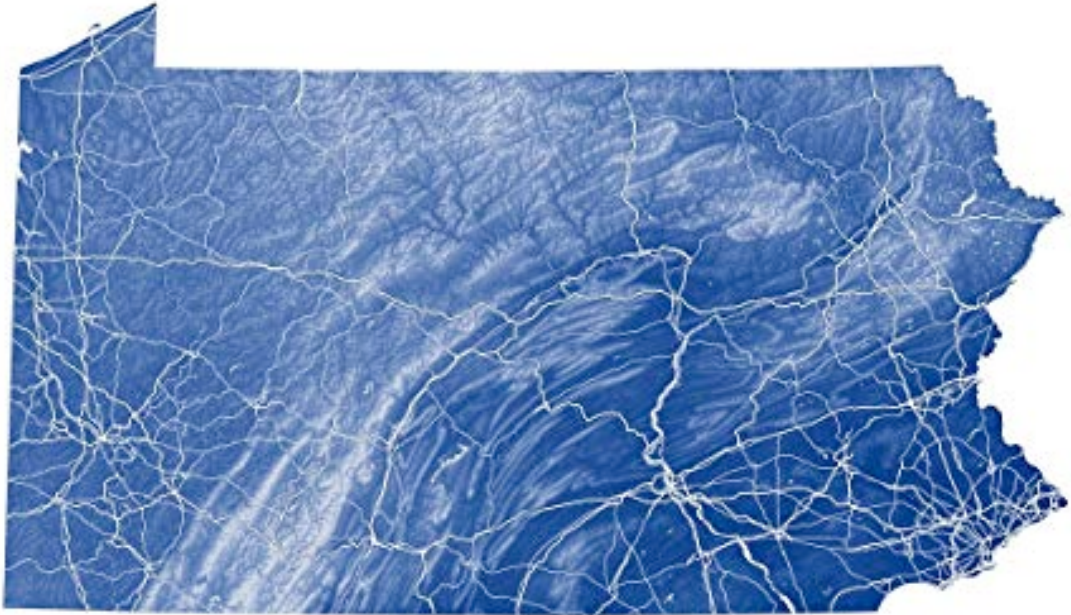
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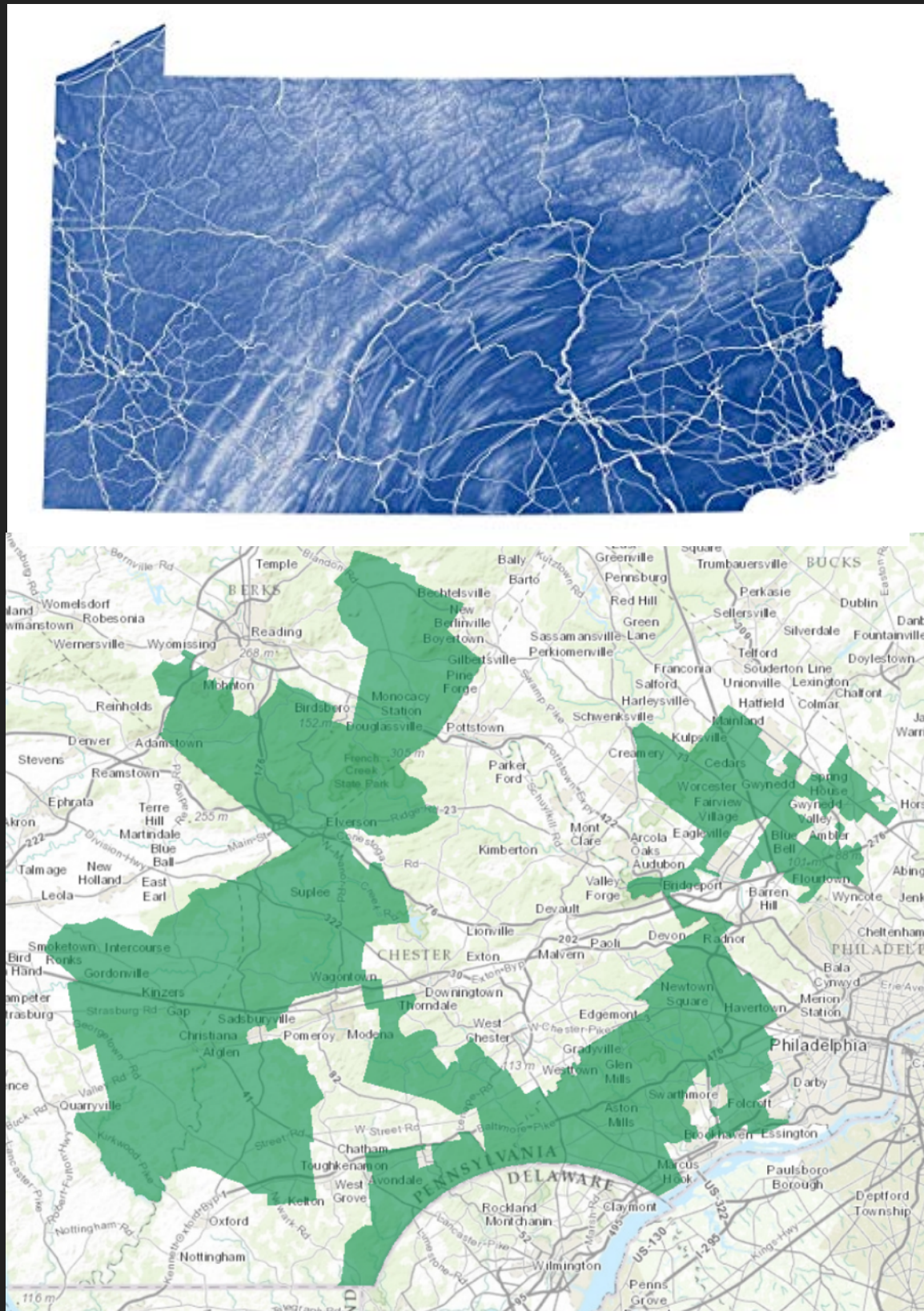
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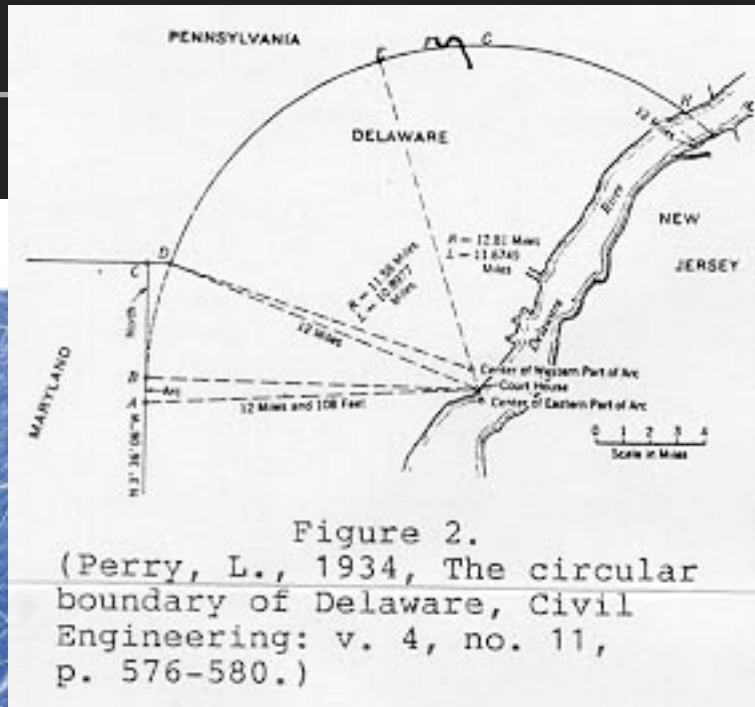
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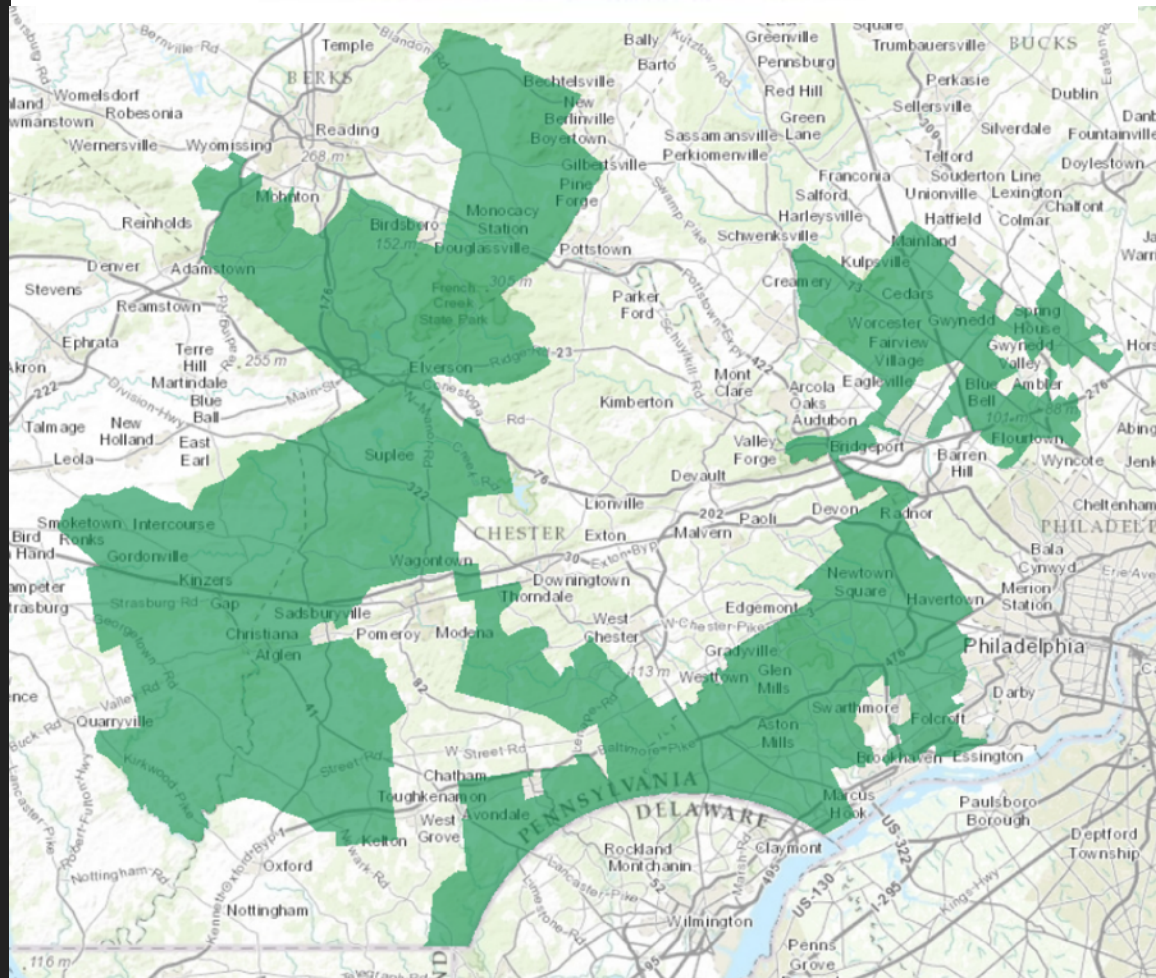
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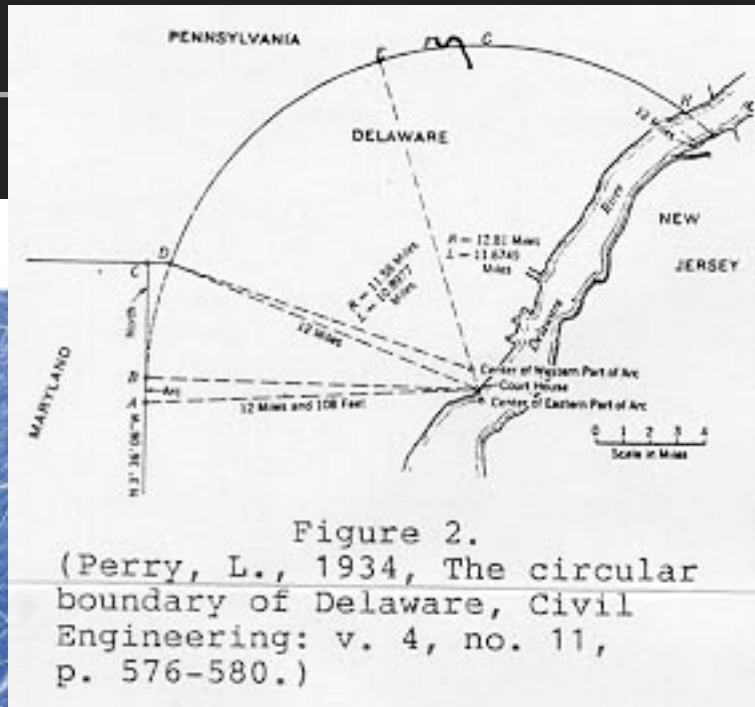




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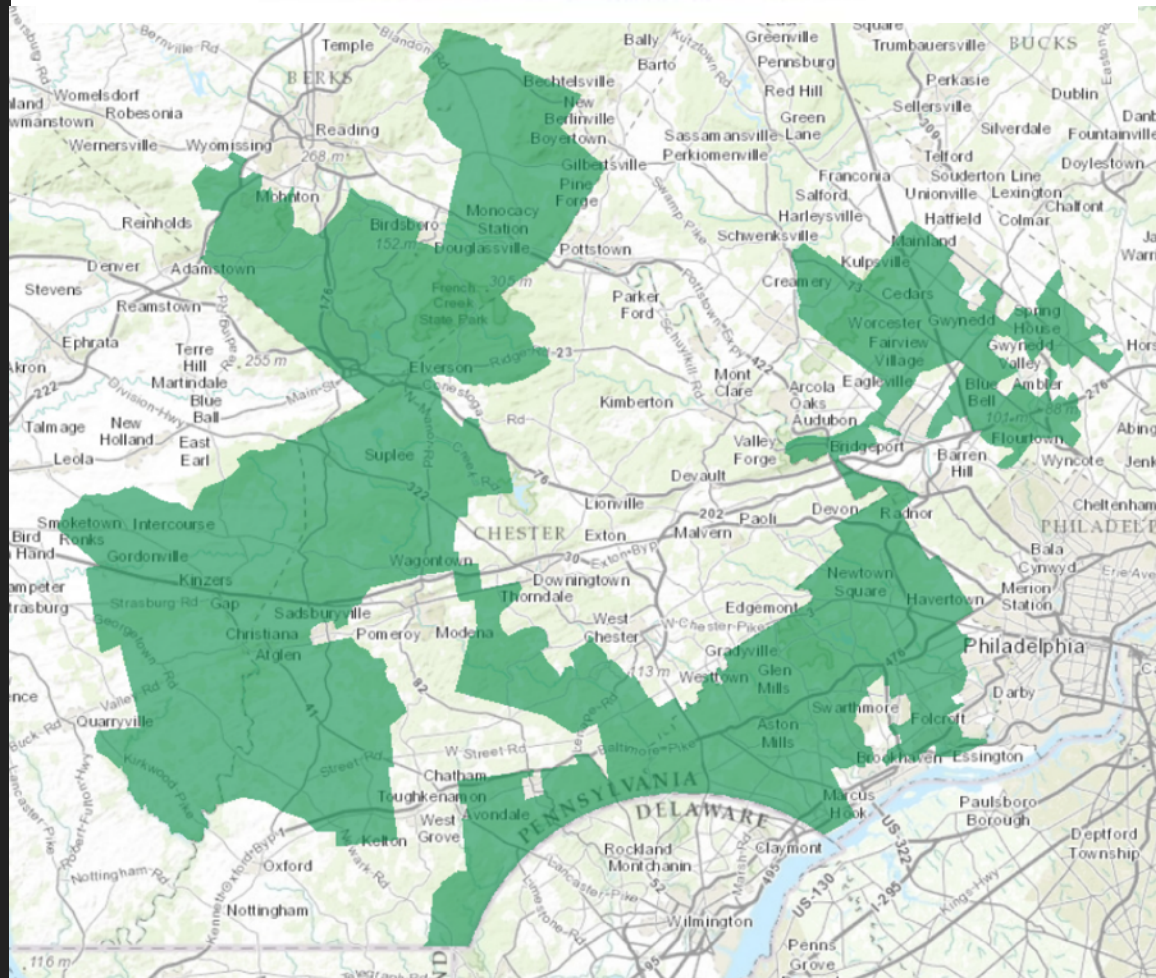
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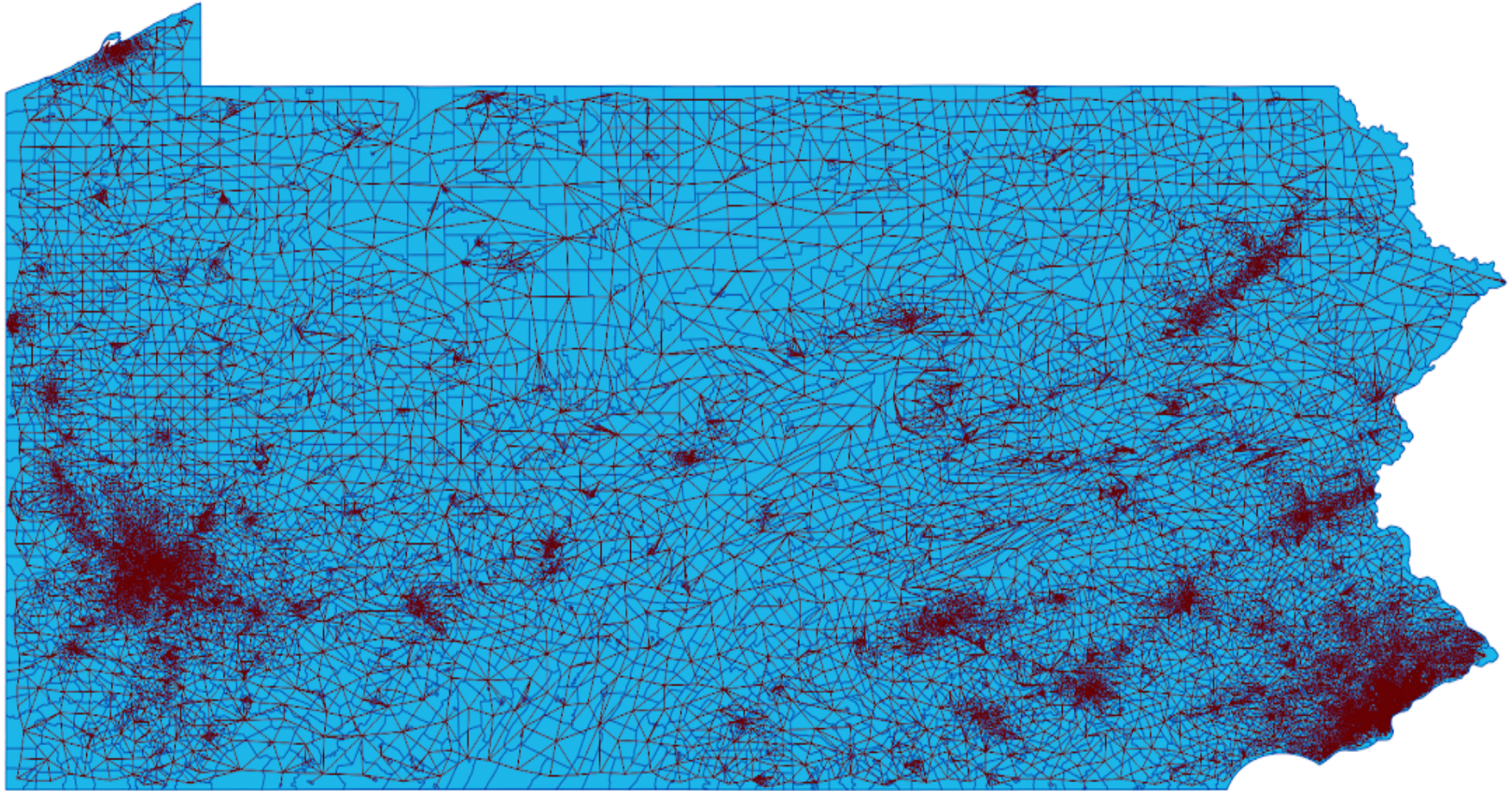
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- ▶ Can't be stored as a round object in GIS, so its technological instantiation in the 2017 Tiger/LINE shapefiles is a 4266-sided polygon

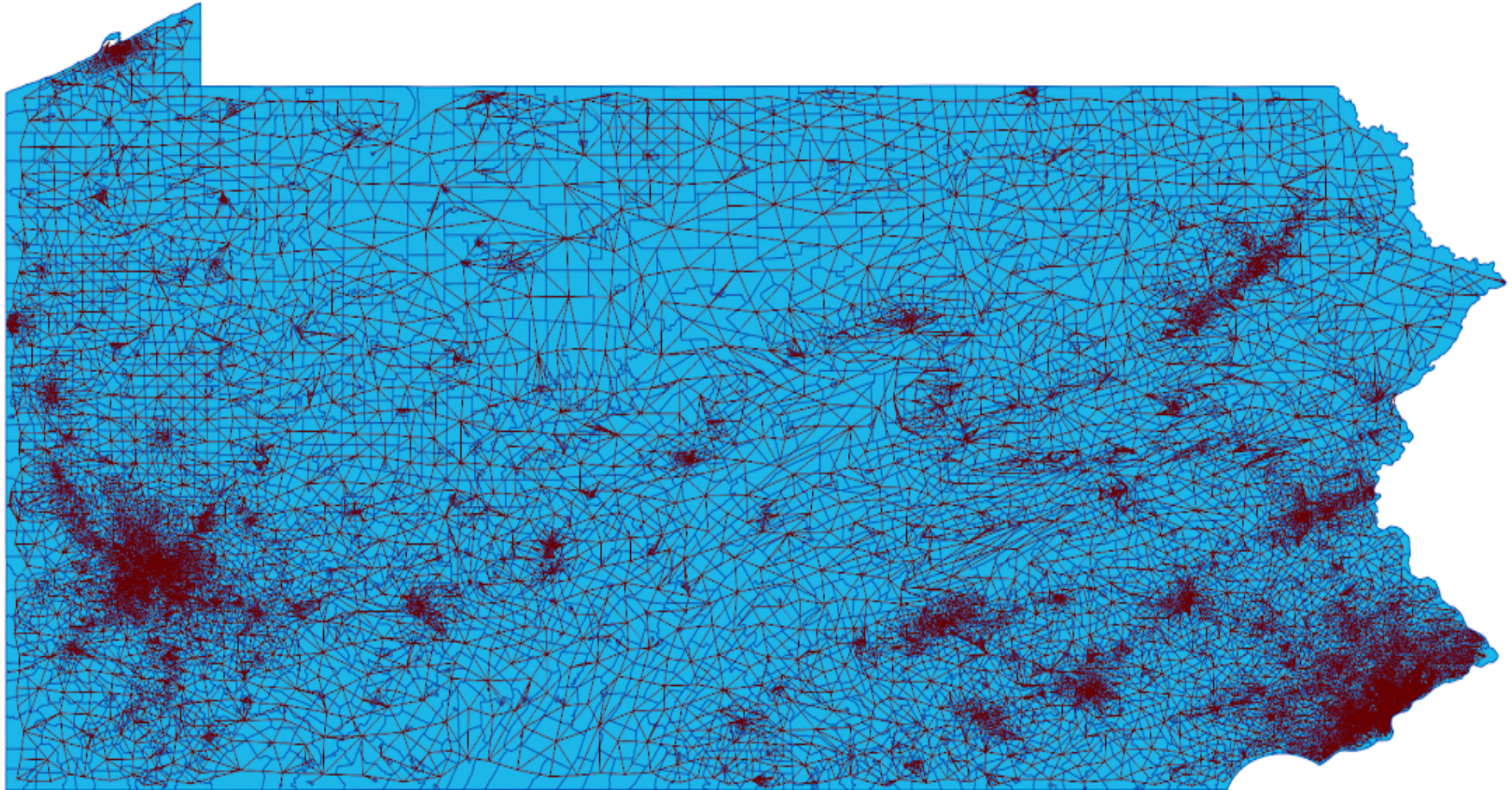


OBJECTS

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Pennsylvania as a precinct network

RULES

WHO THE PEOPLE?

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- ▶ Problem of **virtual representation** lurks behind mechanics of counting - who counts for apportionment? who votes? whose interests are plausibly represented? (Fishkin)
- ▶ As recently as 2016, SCOTUS points to raw Census count as the default basis for redistricting (Evenwel v Abbott)

ANTECEDENTS IN LATE COLONIAL INDIA (B.R. AMBEDKAR)

- ▶ First attempt of “a definite and deliberate kind” to count Untouchables was in the census of 1911, following a reform period when Muslims sought better representation.

Under these tests the Census Superintendents made a separate enumeration of castes and tribes who (1) denied the supremacy of the Brahmins, (2) did not receive the Mantra from Brahmana or other recognized Hindu Guru, (3) denied the authority of the *Vedas*, (4) did not worship the great Hindu Gods, (5) were not served by good Brahmanas, (6) have no Brahman priests at all, (7) have no access to the interior of the ordinary Hindu temple,

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- ▶ Hindu suspicion of caste enumeration: “its aim was to separate the Depressed Classes from the Hindus and thereby to reduce the strength of the Hindu Community”

THE CENSUS

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- ▶ Today multiple Census lawsuits are challenging a new OMB directive to ask respondents for their citizenship status

RULES REDUX

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- ▶ Districts equalize (Census) population, compact and contiguous, preserve counties-cities-communities, and provide opportunities for qualifying minorities to elect a candidate of choice... plus many more local rules

DISTRICTS

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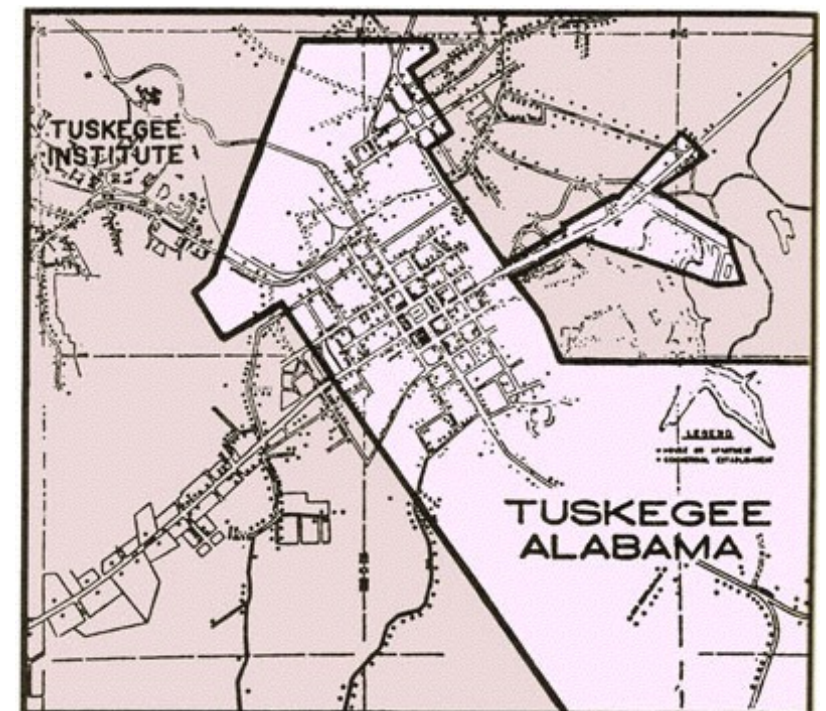
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THE ART OF GERRYMANDERING

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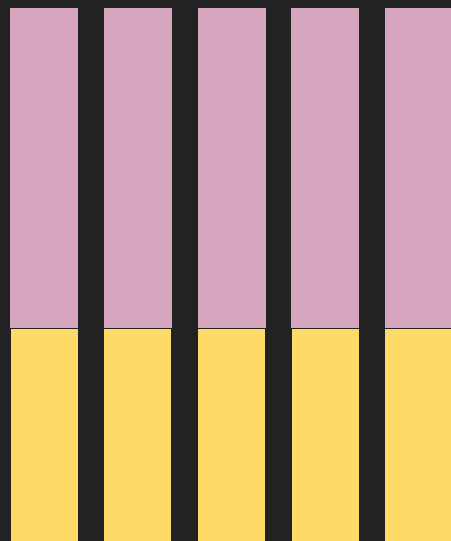
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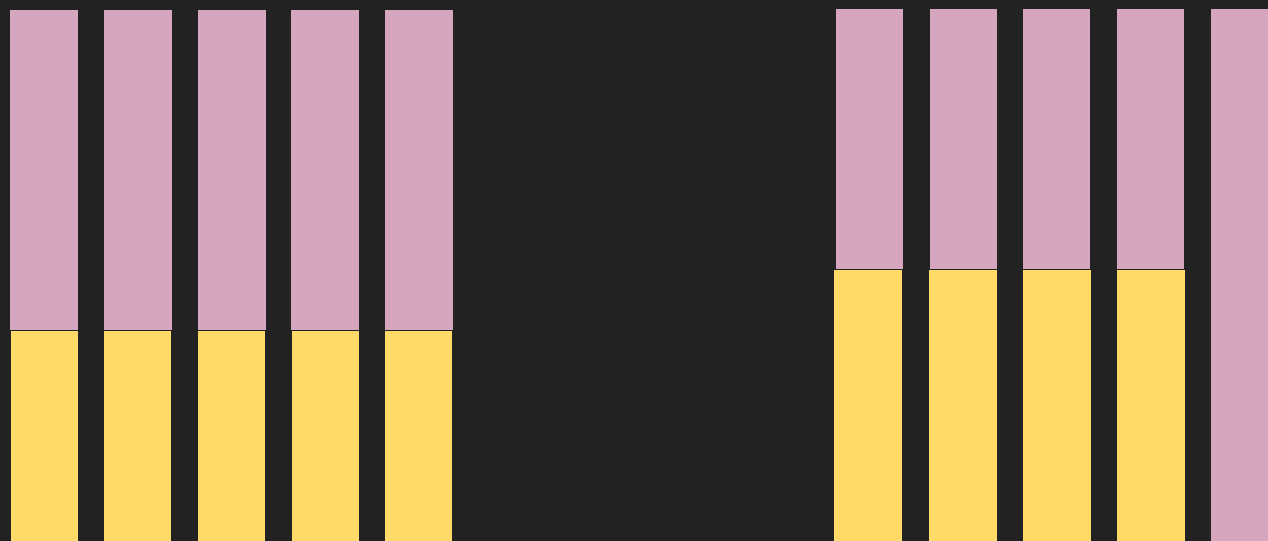
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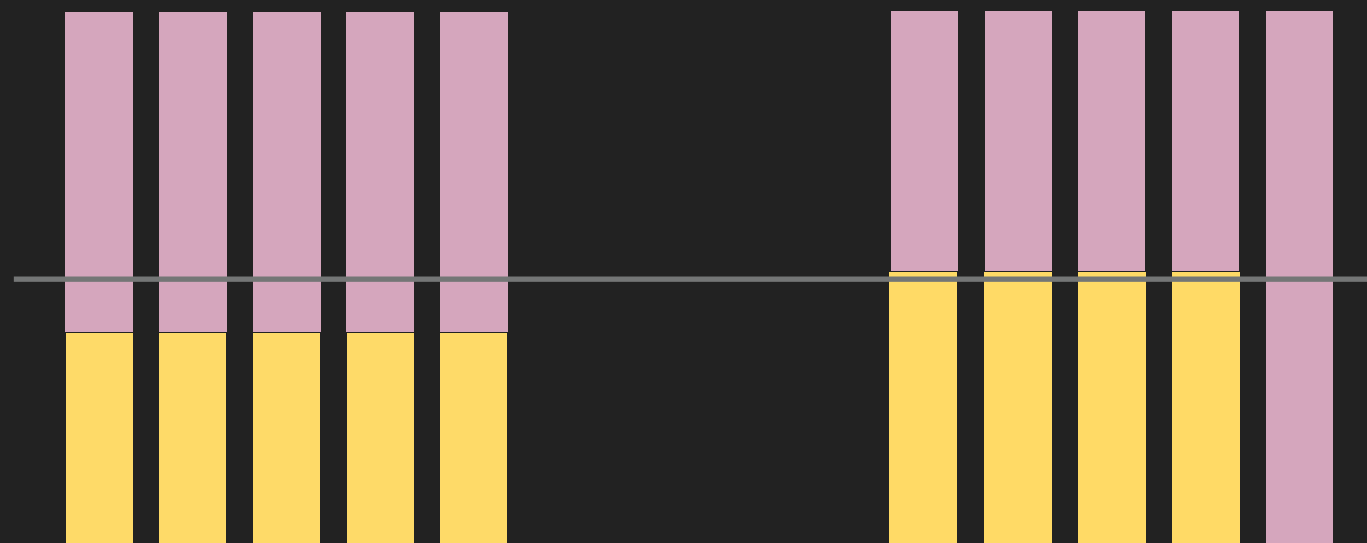
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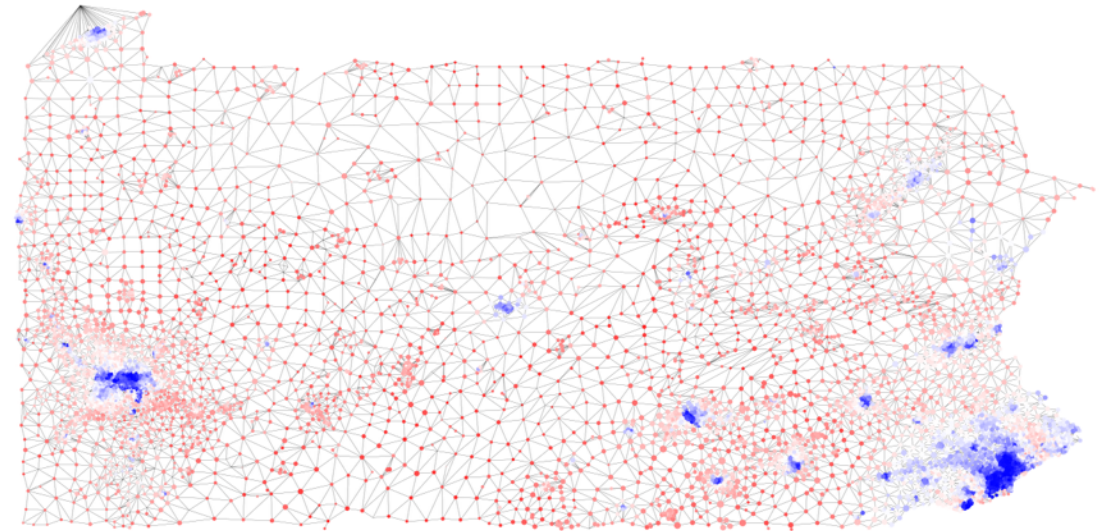


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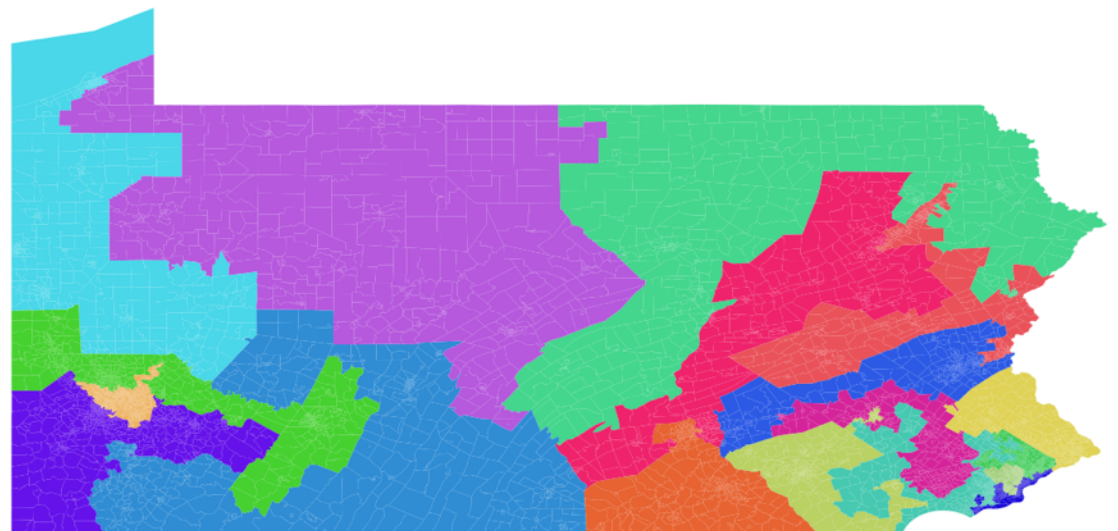
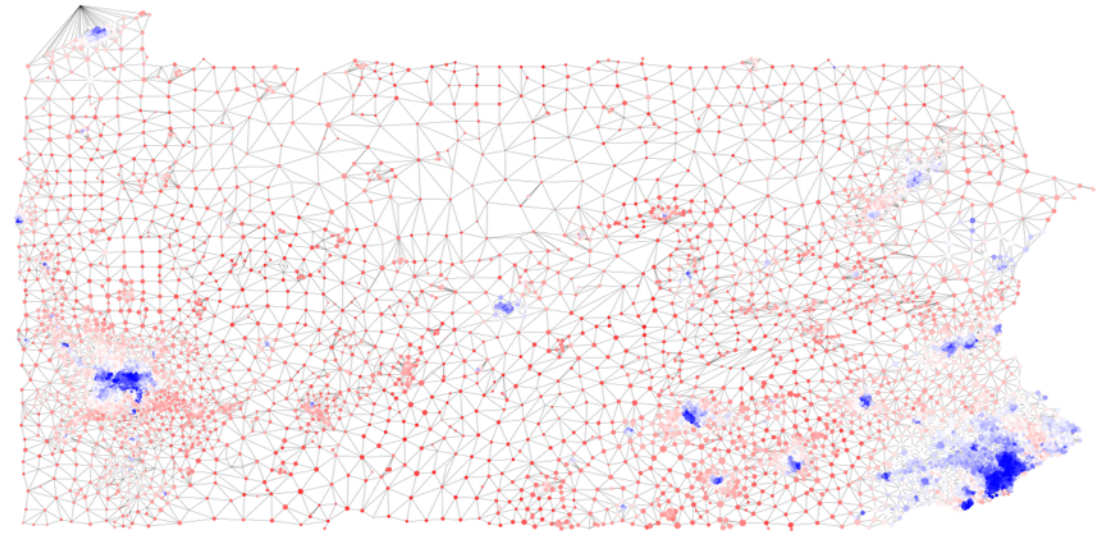
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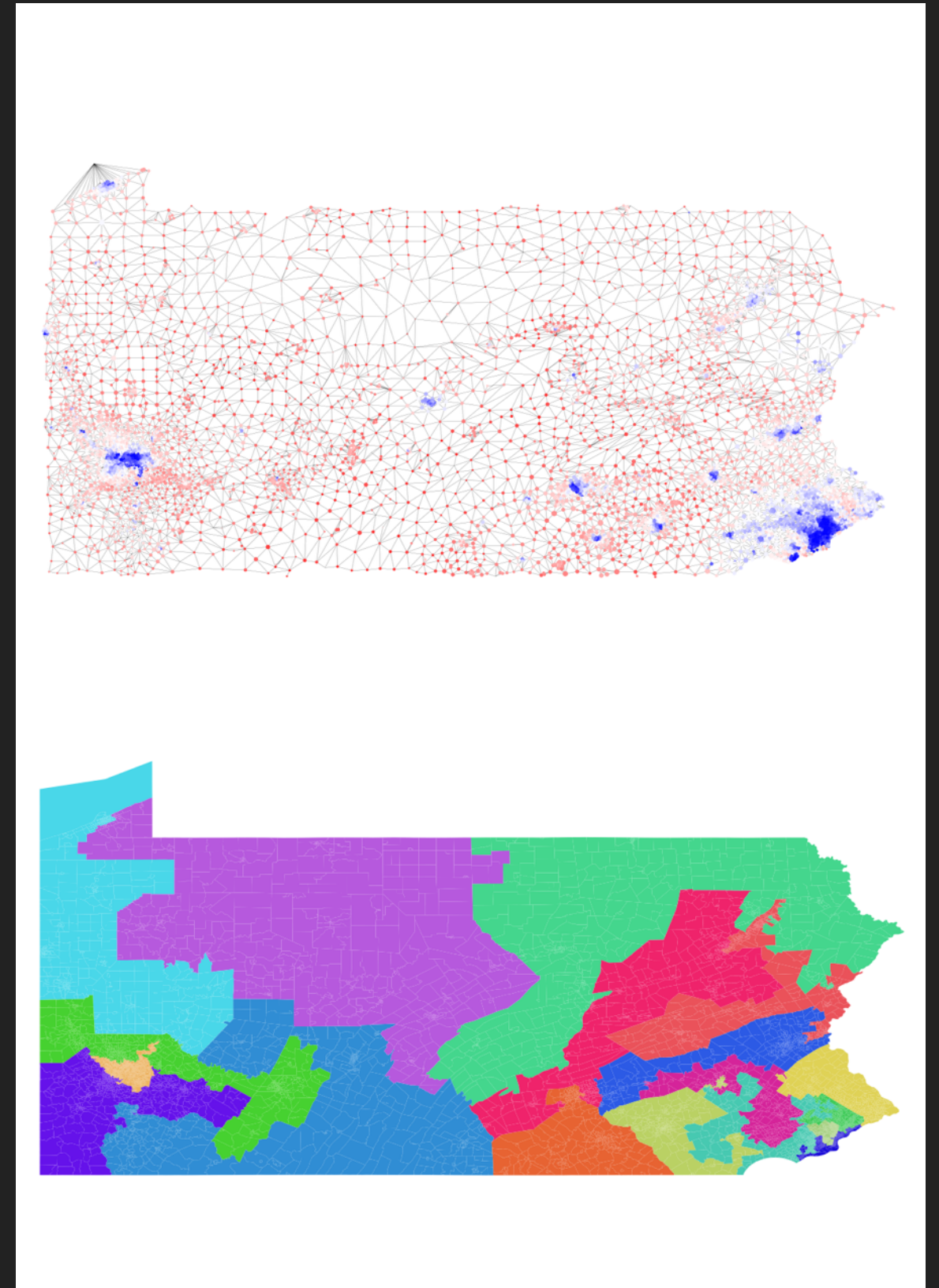
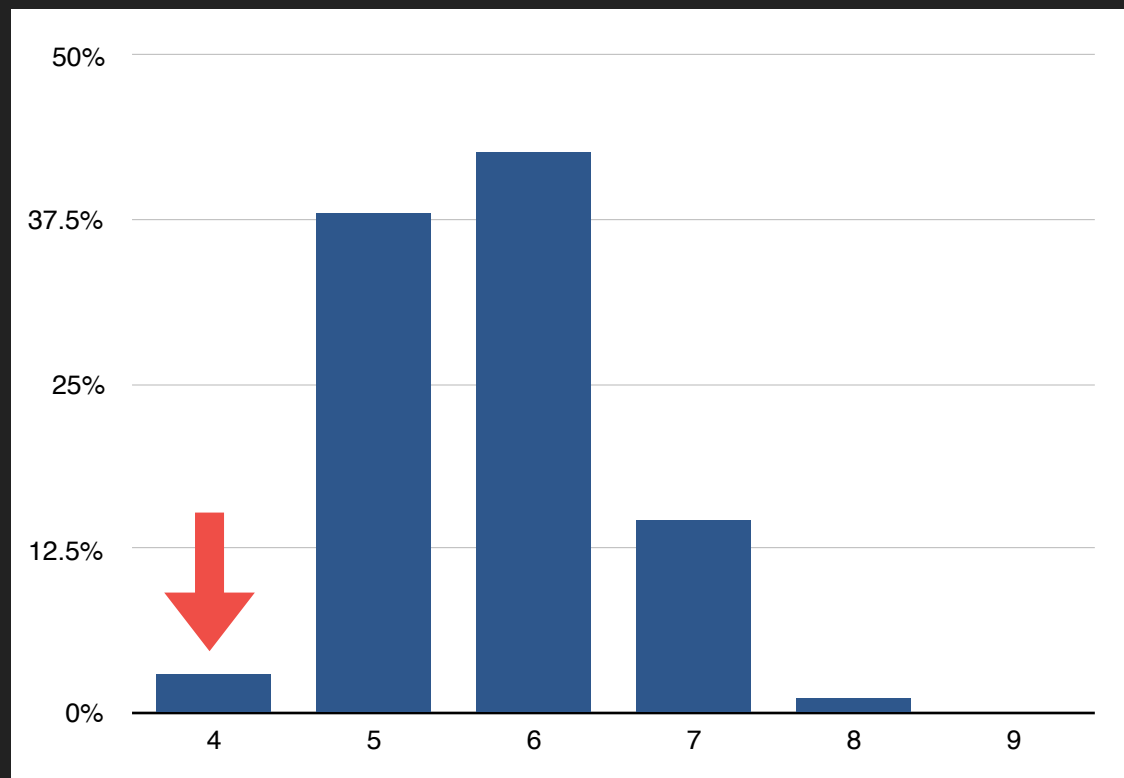
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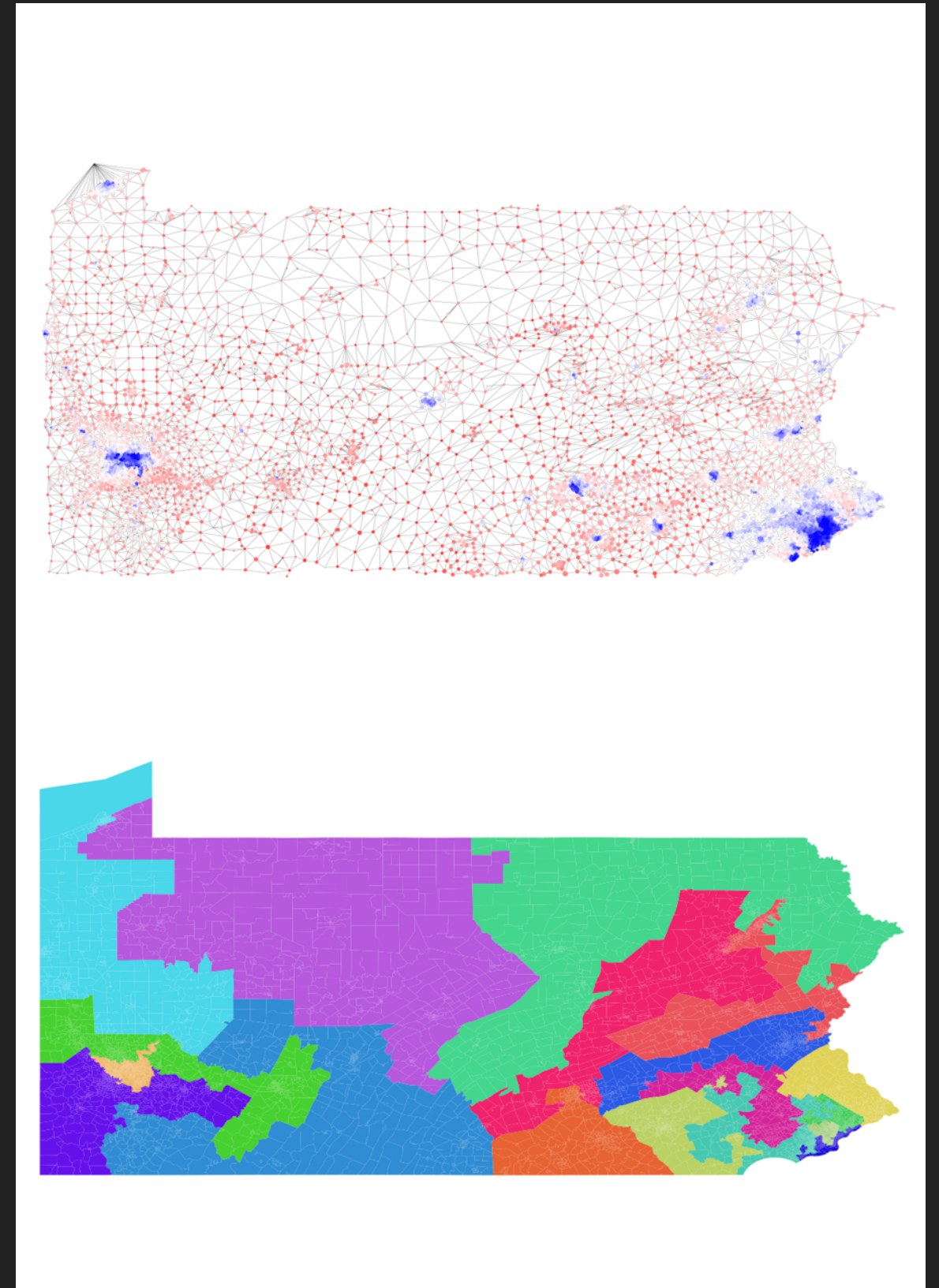
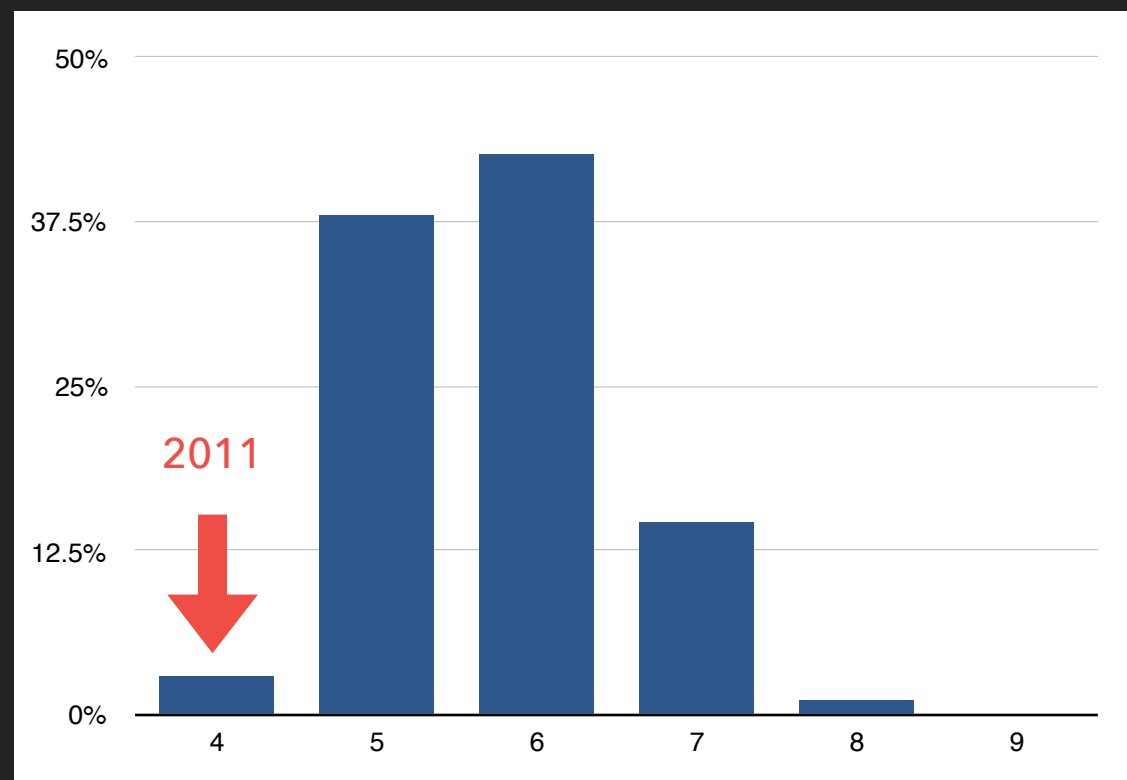
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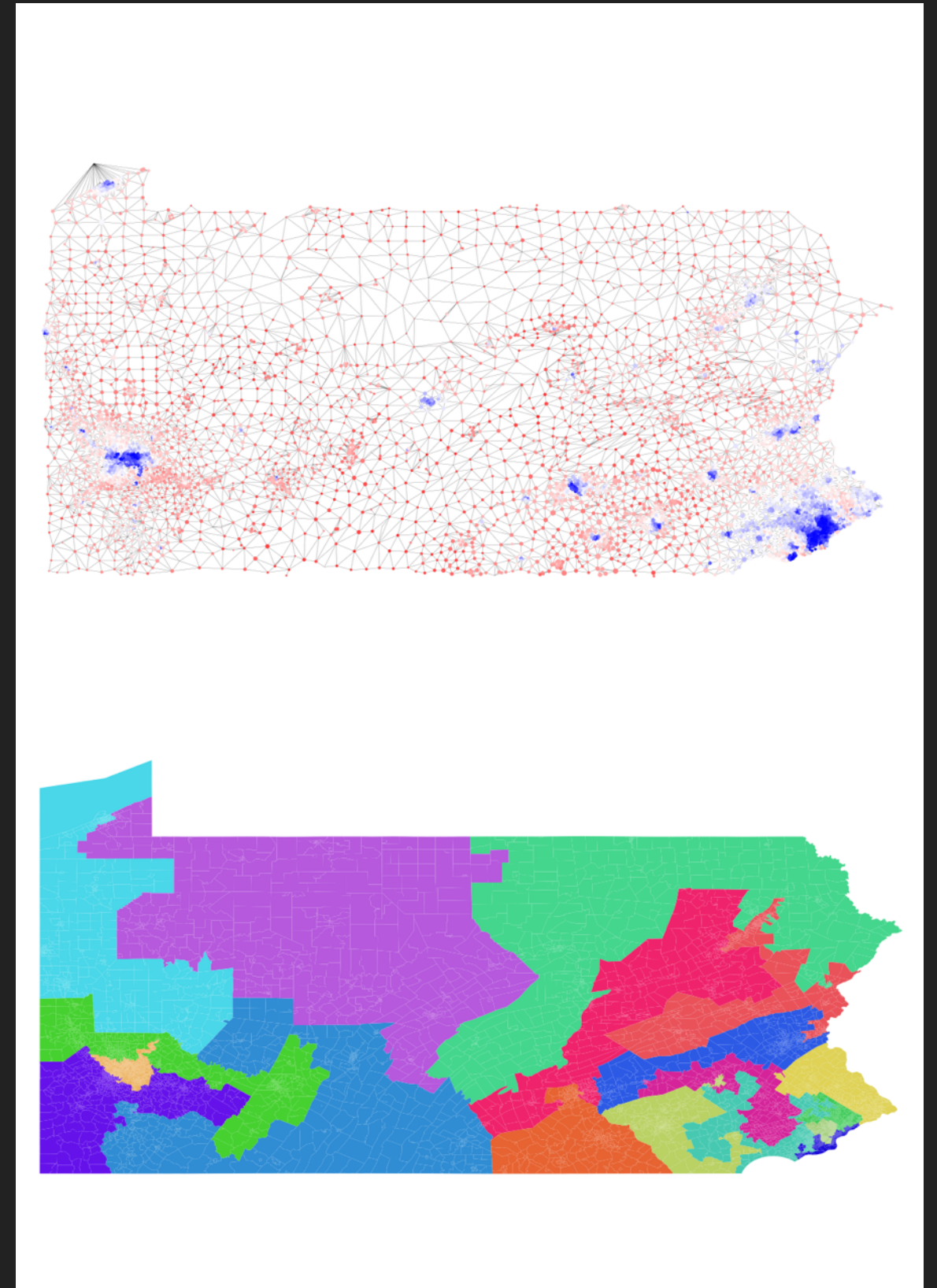
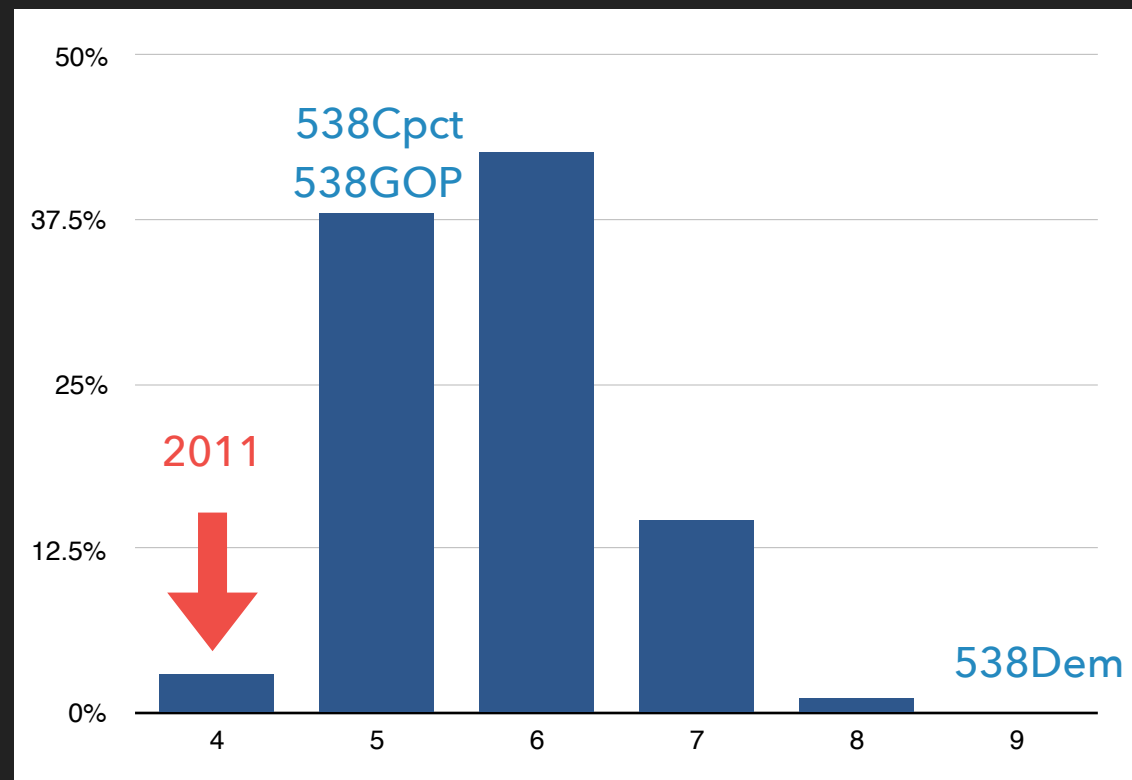
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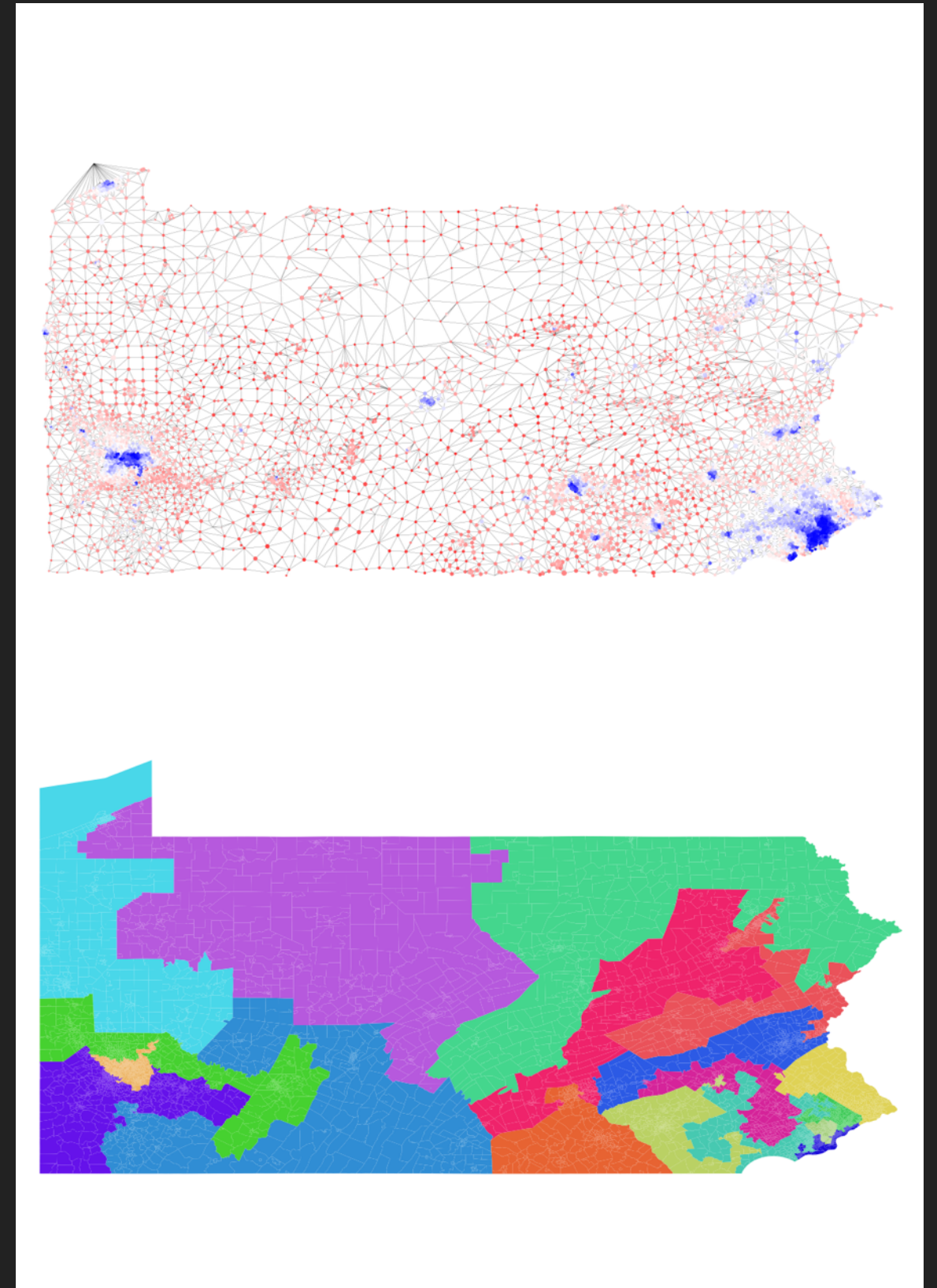
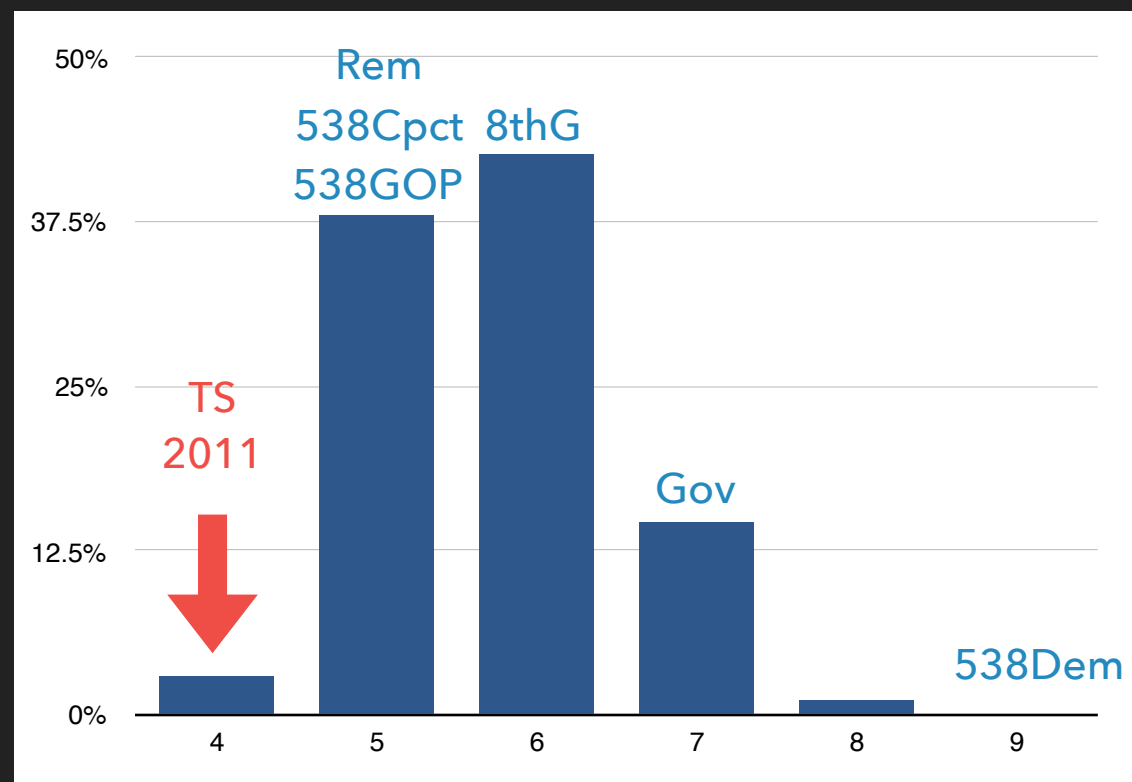
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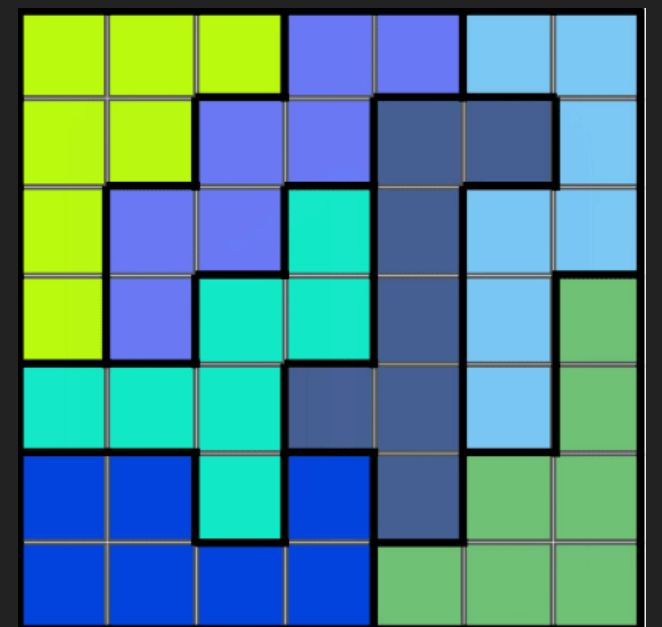


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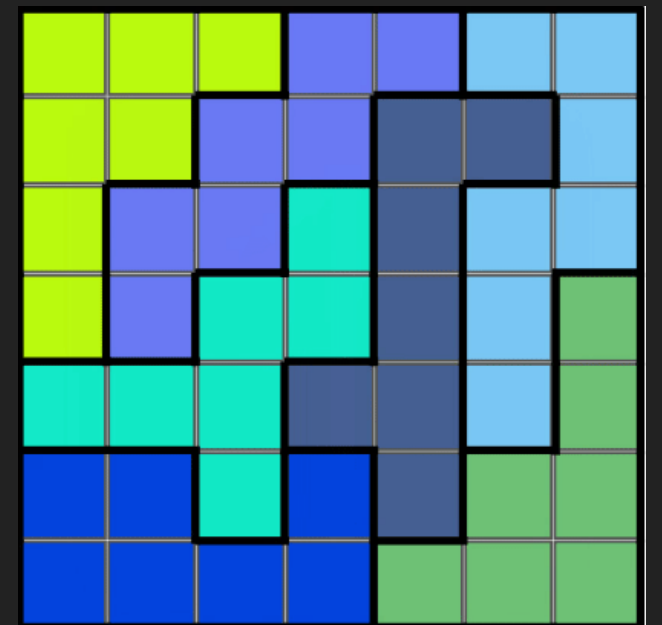


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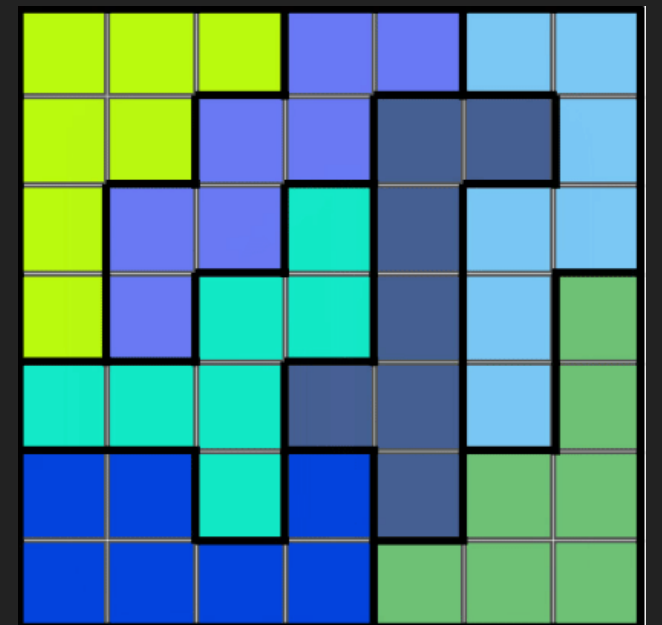
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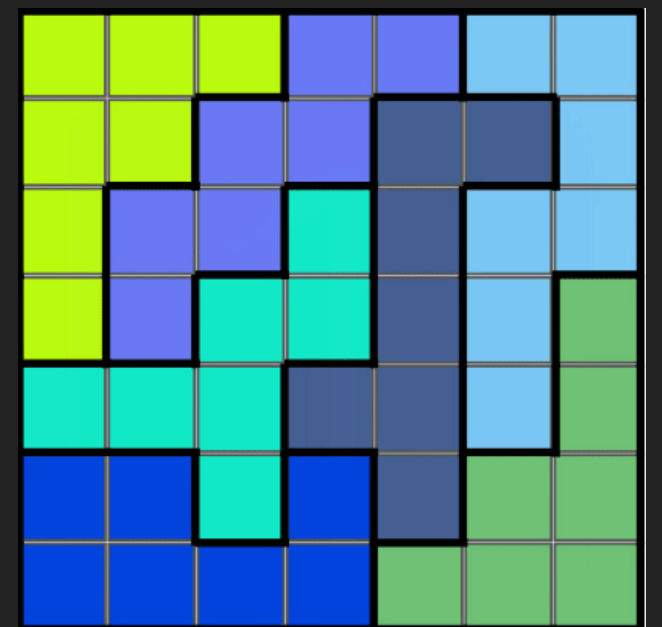
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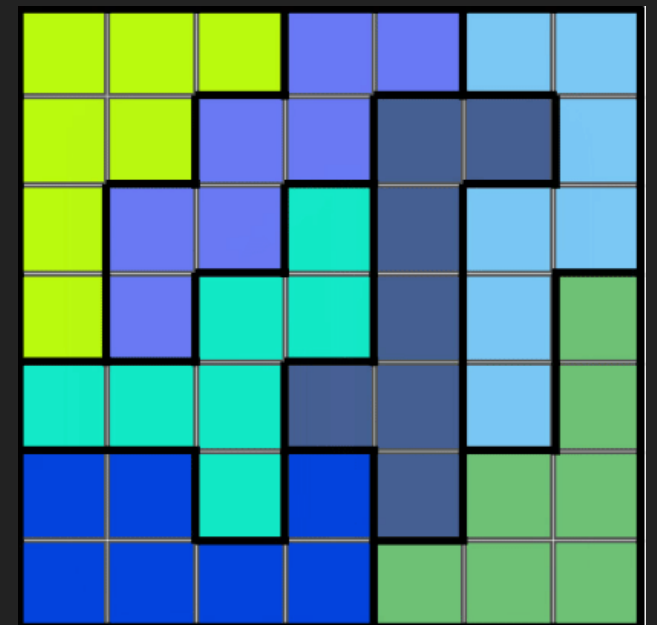
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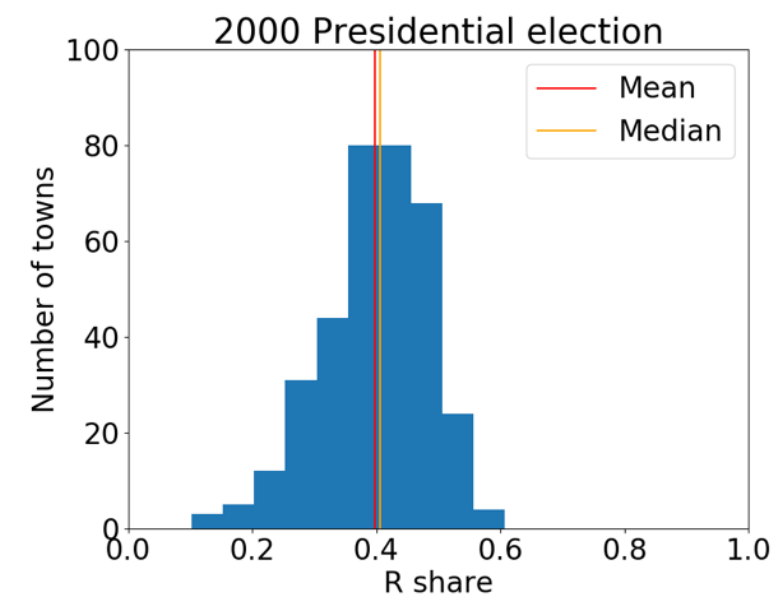
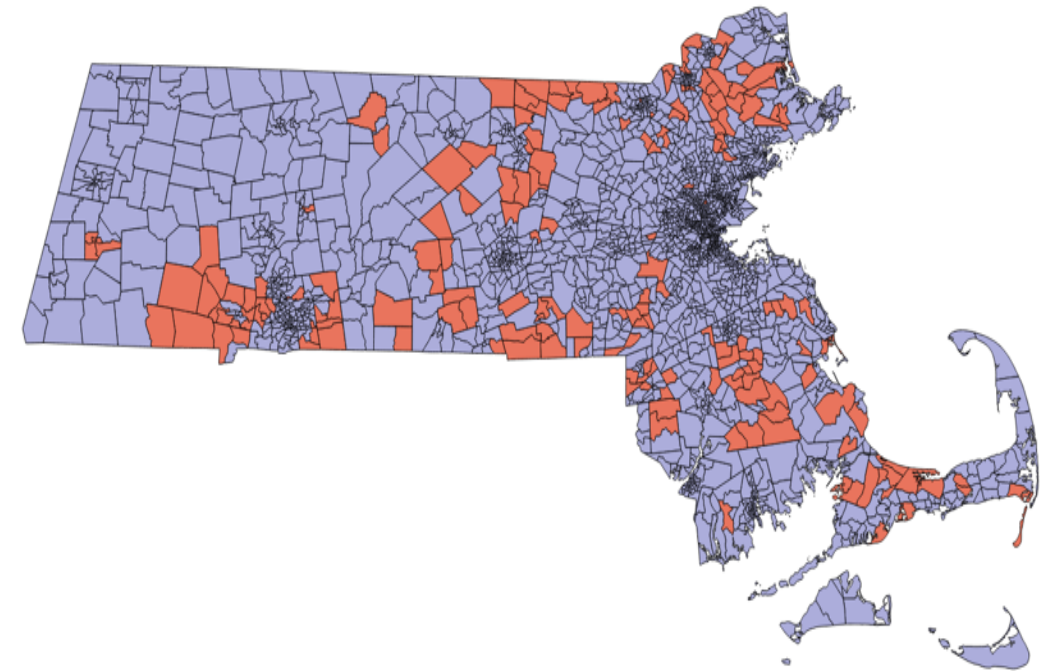
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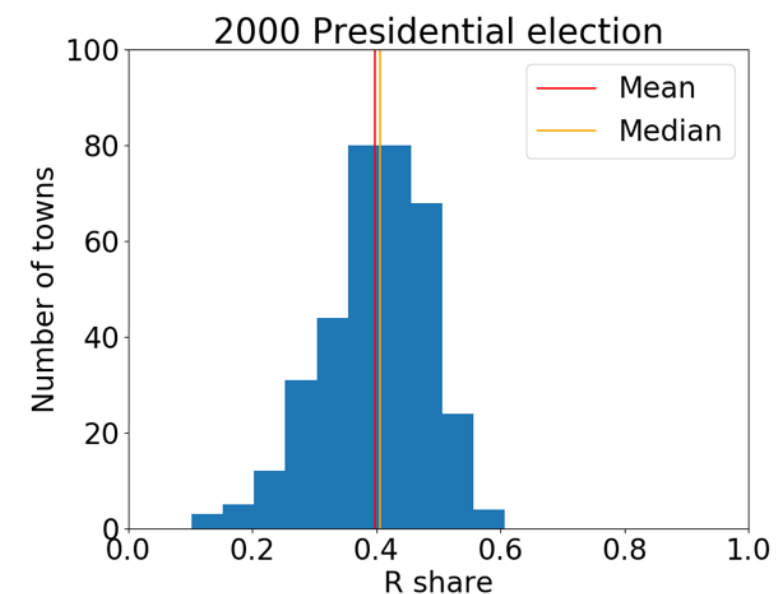
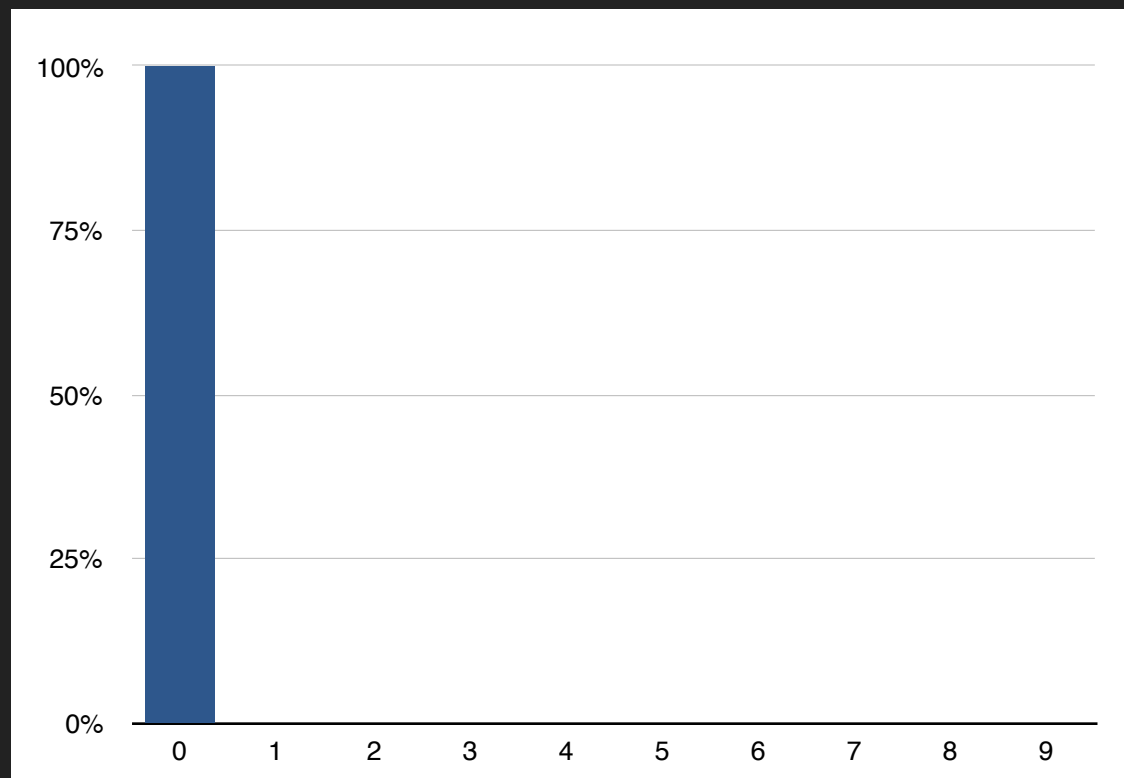
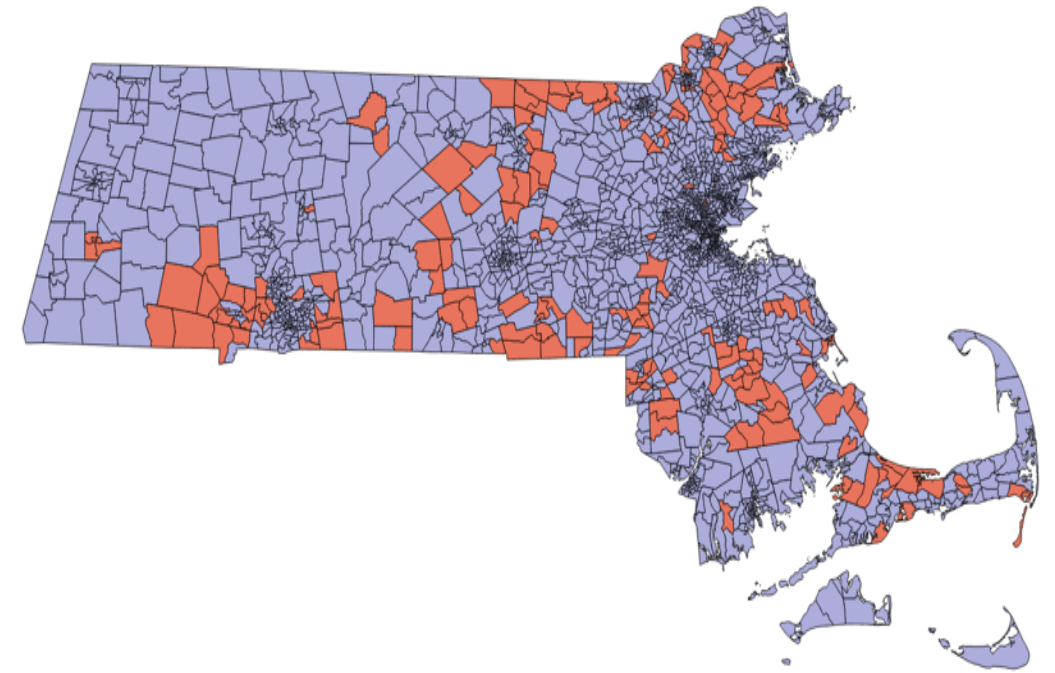
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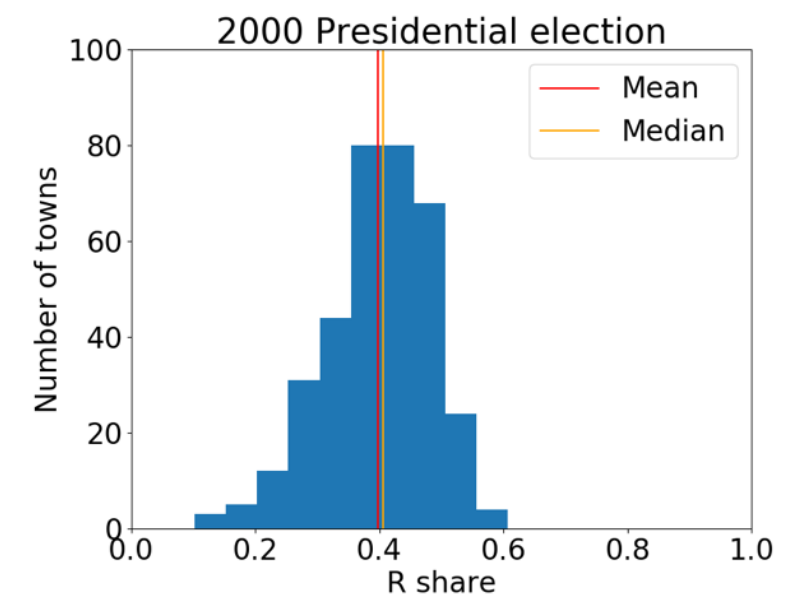
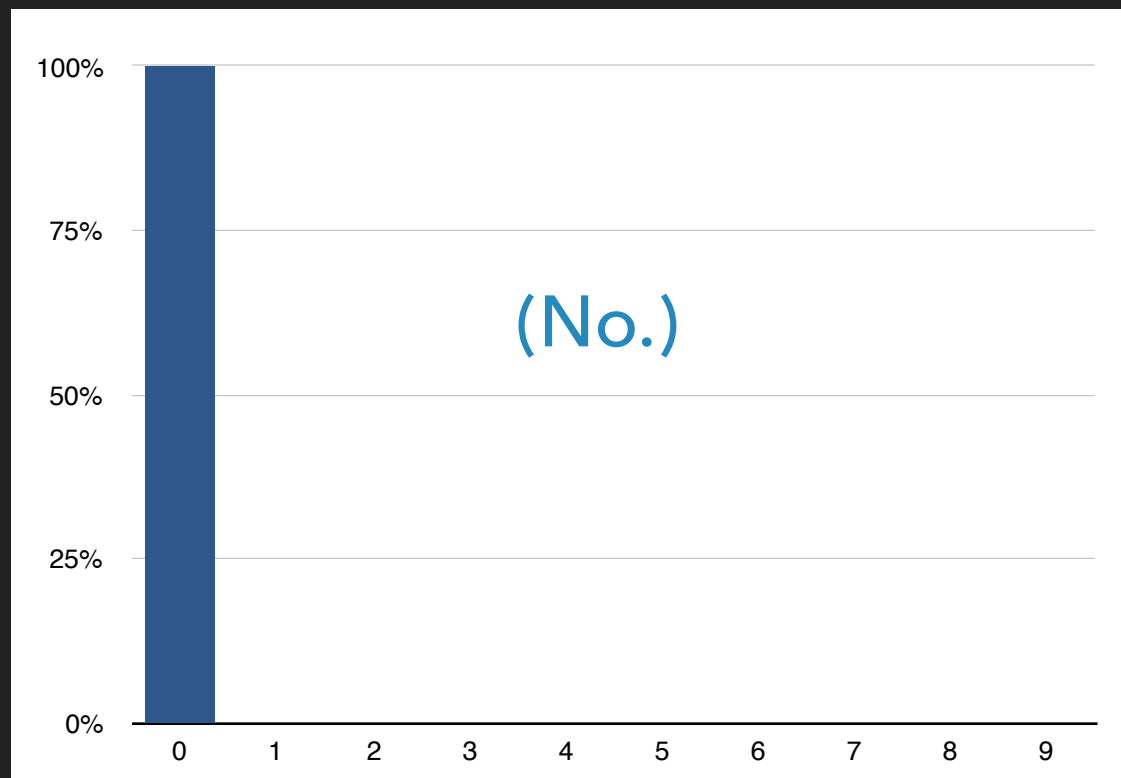
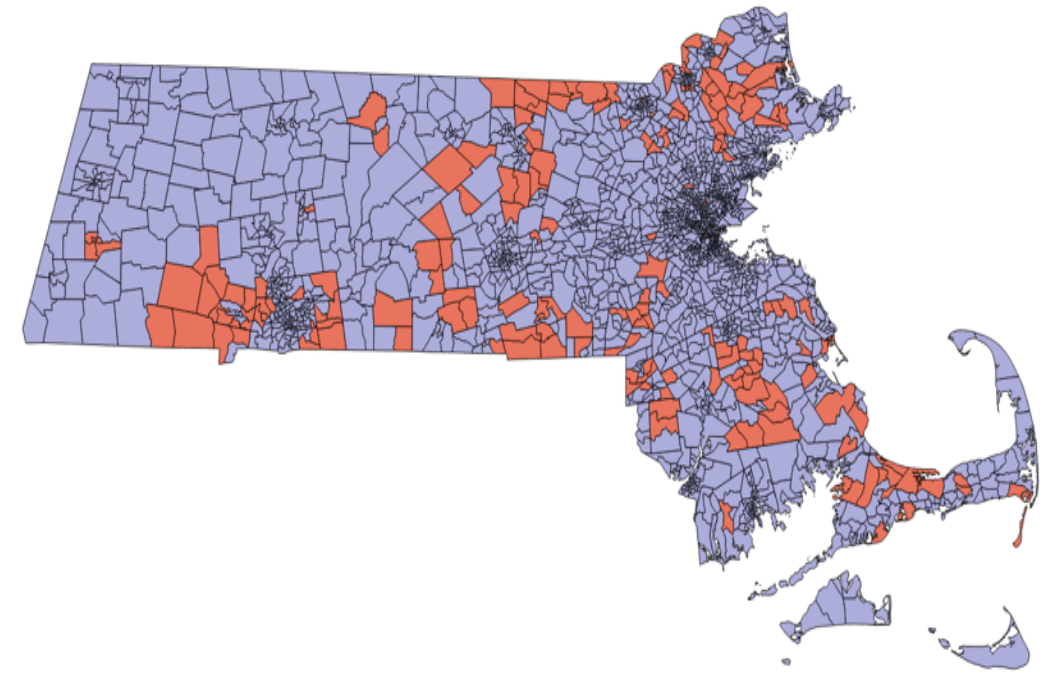
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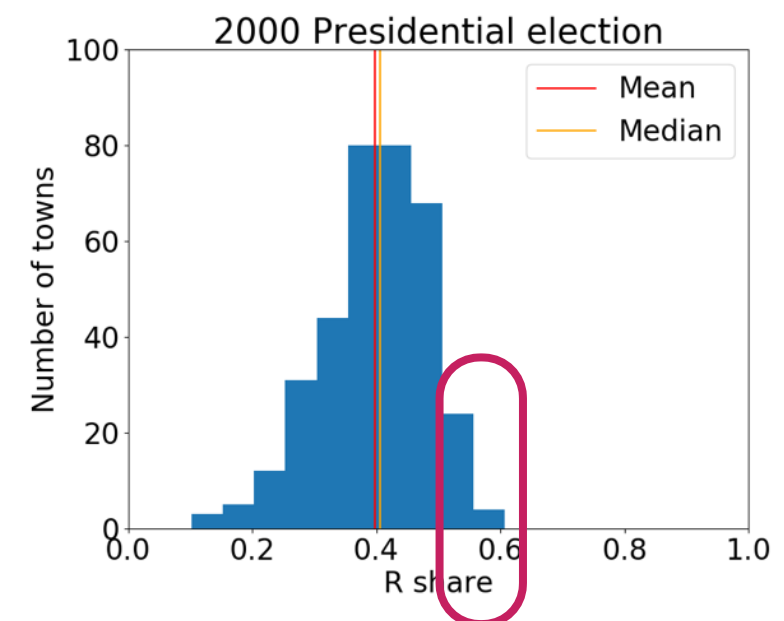
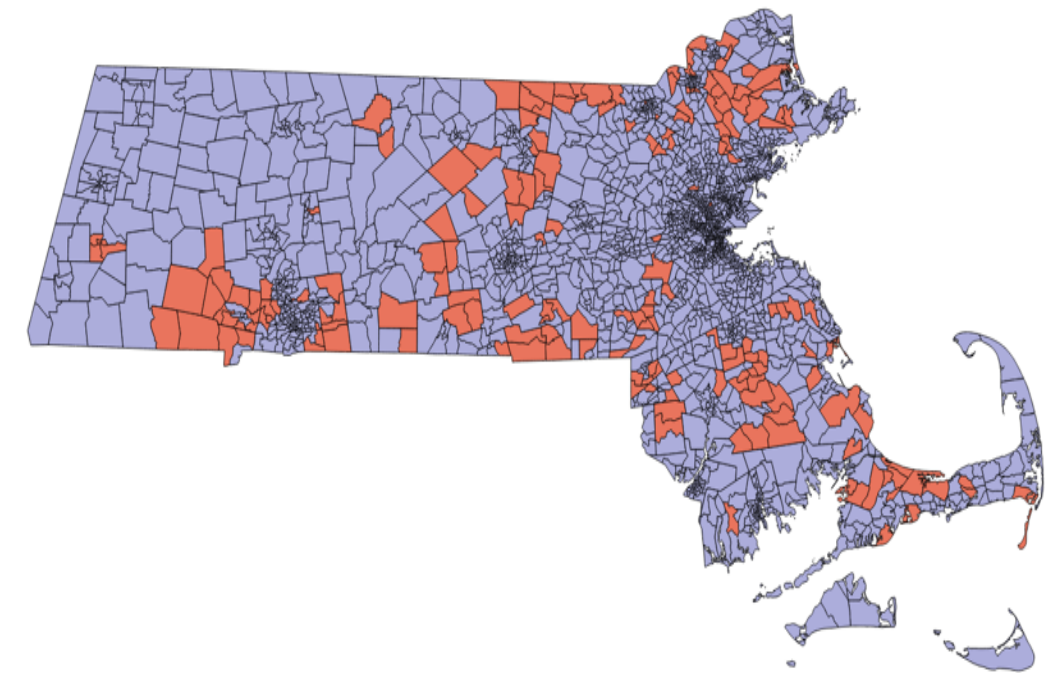
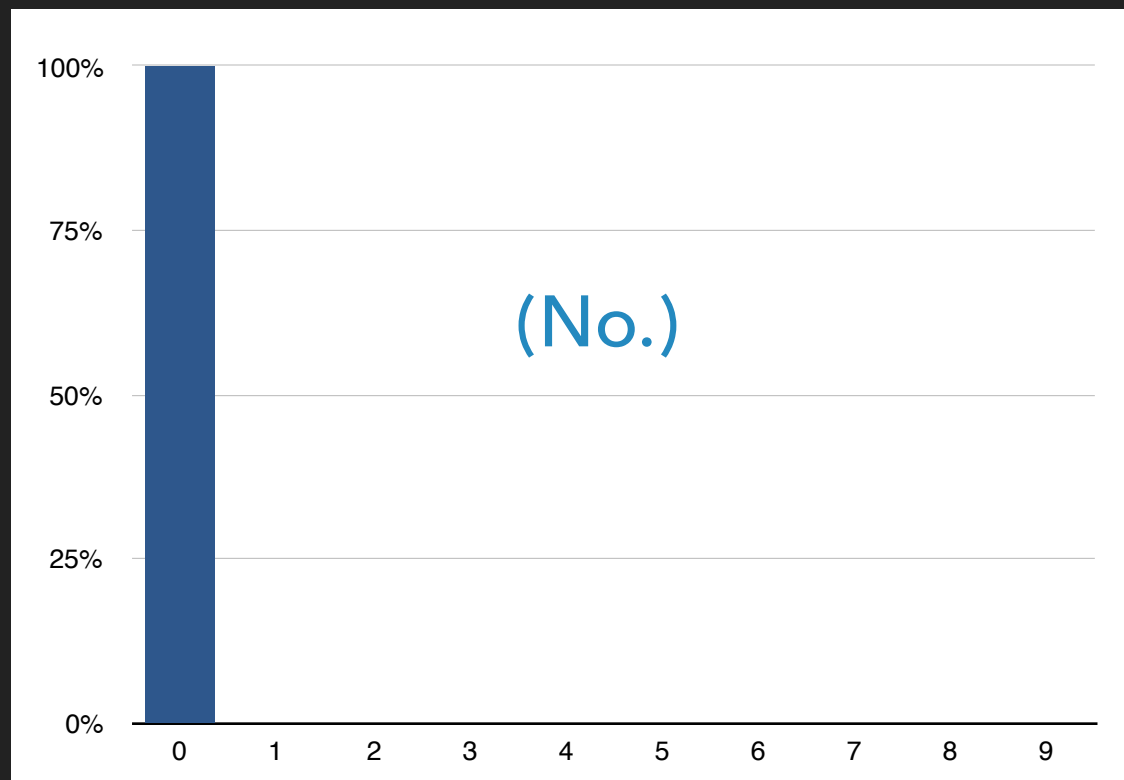
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DISTRICTING AND ITS NORMS

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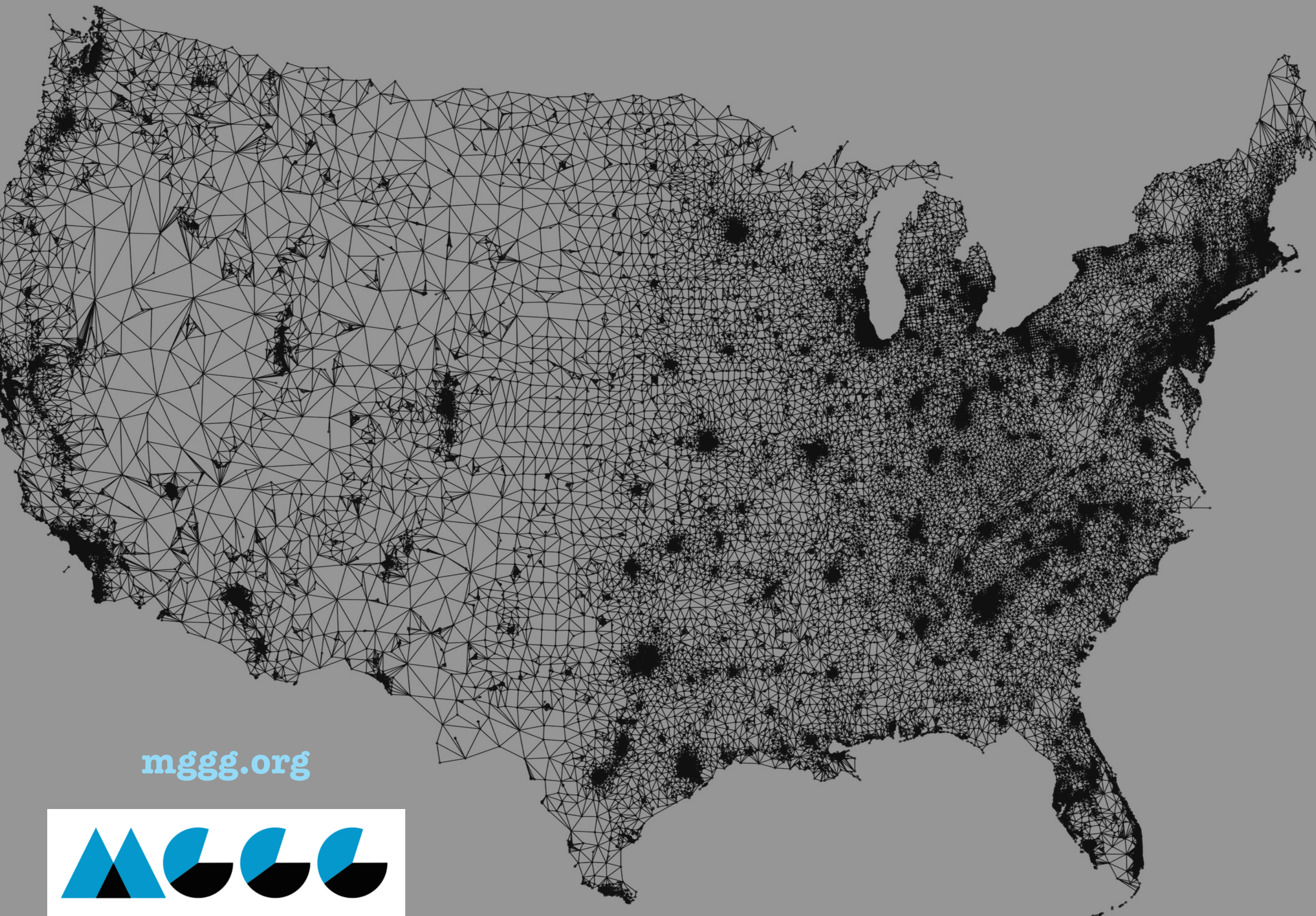
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 Case study for “algorithmic governance”

not to automate, optimize, simulate, or predict
but to verify that a policy
comports with its design principles



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